April 1985

A diode laser source for DIAL methane measurements in coal mines

Richard K. DeFreez

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A DIODE LASER SOURCE FOR DIAL METHANE MEASUREMENTS IN COAL MINES

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A dissertation submitted to the faculty of the Oregon Graduate Center in partial fulfillment of the requirements for the degree Doctor of Philosophy in Applied Physics

April, 1985
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ACKNOWLEDGMENTS

I would like to express my gratitude to Dr. Richard A. Elliott for his support and encouragement during my years at the Oregon Graduate Center. He has been both a teacher and friend to me. I also thank Dr. Fred Holmes for his many helpful technical suggestions. Thanks are also due Dr. John Blakemore for getting me started on this project.

Much gratitude is due to the Homer Research Laboratories of Bethlehem Steel Corporation and the United States Bureau of Mines for continuing material support for this project. I particularly wish to thank Walter Egan and Roger Boos for cooperation that has extended over years.

I wish to thank John Hunt and Robert Cary for their skillful technical assistance. Early on in the project Bruce Odekirk helped me define my goals and lately Mark Foster has given me invaluable assistance in achieving them. I want to thank my friend Robin Fautley for her continuing support. As we have worked together, Mark Gesley has helped me in many ways.

To my wife, Toni, and my son, Dan, I dedicate this work. They have been my inspiration to succeed.
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The research reported in this dissertation was directed toward the development of a coal mine methanometer source. The project encompassed two tasks. The first was a study conducted to determine if room-temperature injection lasers could be used as the source for a DIAL methanometer for coal mine applications. As part of that study, prior DIAL measurements of methane were reviewed and the measurement technique was explored in a general way. The absorption spectroscopy of methane was then examined in detail and found to contain an appropriate absorption feature near a wavelength of 1.65 μm provided the spectral width of the light source was approximately 0.2 cm⁻¹. As an additional part of the study the operating characteristics of broad area high optical output InGaAs/InP injection lasers were examined. A detailed calculation of the requirements for a diode laser DIAL measurement of methane in a coal mine was then performed. By comparing the observed diode laser properties with the DIAL requirements, it was found that
broad area InGaAs/InP injection lasers were suitable in most respects for coal methane measurements. The exception was the diode laser spectral bandwidth. It was found to be some 400 times too large.

The second task was the design and fabrication of an external grating cavity to reduce the bandwidth of the injection lasers. The optical design of an off-axis parabolic mirror grating cavity was developed. Geometric optics was used to determine the physical parameters for an external cavity which would produce the desired spectral bandwidth of 0.2 cm\(^{-1}\). The fabrication and performance of this external resonator source is described. Measurement of the source linewidth showed it to be two to three times larger than the design value. An explanation of the resultant bandwidth based on coupled mode theory is presented. In summary, an external grating cavity for a diode laser was designed, assembled, and tested. It was shown to approximate the optical properties required for a DIAL coal mine methane measurement.
1. INTRODUCTION

The presence of noxious and explosive gases in underground mine atmospheres has always posed a serious threat to the well-being of miners. Increases in mining mechanization, particularly since World War II, have enlarged the gas burden facing miners\(^1\). In the United States, this increased burden has stimulated federal mine-safety legislation\(^2\). In turn, these same regulations have reduced the productivity gained through mechanization.

Nearly two-thirds of all underground U.S. coal tonnage is extracted using continuous mining machines in room-and-pillar mining operations\(^1\). As a result of the Mine and Safety act of 1969\(^2\) and various state laws, present practice in the room-and-pillar mine is to stop mining every twenty minutes to measure the concentration of methane gas at one foot from the working face. After the mining machine is withdrawn, temporary roof supports are installed to the working face so that a miner can approach the face and measure the methane concentration with a handheld catalytic combustion methane detector and/or flame safety lamp\(^3,4\). When the measurement is completed, the temporary roof supports are removed and the mining machine begins mining again\(^5,6\). Obviously, this procedure reduces productivity and is in itself a safety hazard as temporary roof supports can well be dangerous.

It has been estimated that remote methane measurements could provide up to a 5 percent improvement in room-and-pillar coal mining productivity\(^7\). Such a pro-
ductivity increase would represent about 11,000,000 tons of coal annually in the U.S. alone. The ability to make remote methane measurements would also be useful in other underground mines, for example in salt mines.

The need for a remote measurement of methane concentration at the working face of an underground coal mine was identified at Bethlehem Steel Corporation in the spring of 1977. Specifications for a methane measurement instrument were drawn up in 1978 at Bethlehem Steel Corporation's Homer Research Laboratories (HRL), and evaluation of remote gas sensing techniques was begun. That evaluation process included contacting Prof. R. L. Byer, well known in remote detection of pollutants, about the potential use of LIDAR (light detection and ranging) methods. In August of 1978, Prof. Byer wrote that remote methane detection could be achieved by differential absorption LIDAR (DIAL) techniques.

As of 1978, Raman-shifted neodymium glass, Raman-shifted Nd:YAG, and Erbium doped YAG (Er:YAG) were all considered as potentially feasible sources for the stated task. Er:YAG was selected as the simplest of these for experimental work, which was carried out at HRL by the present author in the summer of 1979.

The work at HRL in 1979 demonstrated that methane could be remotely detected and measured in a laboratory, using the DIAL technique, an Er:YAG source, and Mie retroreflection from coal dust. However, the Er:YAG laser is inherently a device of low conversion efficiency, with a theoretical upper efficiency limit of only a few percent. Moreover, a flash lamp driven device (such as the Er:YAG laser used at HRL in 1979) requires high voltages and driving currents. Redesign to satisfy the Federal Code in terms of safety hazards would clearly be difficult.
Fortunately, a different kind of laser source for a wavelength compatible with methane absorption (1.65 μm) became realizable at about the time the 1979 HRL study was completed. This alternative is a sophisticated form of semiconductor injection diode laser. Room-temperature injection diode lasers for the "long-wavelength" region from 1 μm to 1.7 μm have been reported only during the last few years\textsuperscript{12-18}. Thus a study\textsuperscript{19} was initiated by Bethlehem Steel Corporation at the Oregon Graduate Center (OGC) at the end of 1980 to determine the feasibility of using an injection laser as the source in a portable methanometer.

During that 9 month study, it was found that In\textsubscript{0.53}Ga\textsubscript{0.47}As diode lasers could indeed be suitable as a methanometer source if their spectral output could be modified to match the requirements of a DIAL measurement. The study indicated the proper modification could be realized by mounting the semiconductor laser in an external diffraction grating tuned cavity and design parameters for such a cavity were specified.

Subsequently in 1982 Bethlehem Steel Corporation contracted with the U.S. Bureau of Mines (Contract No. H0123031) to build a dual wavelength light source for a proof of concept demonstration in collaboration with the Oregon Graduate Center. This thesis discusses the DIAL measurement requirements, and describes the diode laser characteristics, optical design of the external cavity, and the implementation of the design. The work on the external diode laser cavity source described here is, to this author's knowledge, unique in four ways. First, it is the first planned use of room-temperature diode lasers for a DIAL source. Second, the resonator is the first third-order aberration-free off-axis external cavity diode laser built. Third, the cavity is the first to use diamond-machined optics for an external cavity diode laser. Fourth, it is the first wavelength dispersive external grating diode laser with
closed loop electronic wavelength control capabilities.

The organization of the thesis is as follows. Chapter 2 presents an overview of the DIAL technique for remote sensing. In Section 2.1, DIAL is compared with, and contrasted to, other LIDAR methods. This is accomplished through an explanation of the fundamental LIDAR formula, Equation 2.1. Section 2.2 explores the background of range resolved DIAL and describes its potential application in coal mines. A history of previous attempts to remotely monitor methane is given in Section 2.3.

Chapter 3 deals with the spectroscopic considerations pertinent to a DIAL methane measurement in a coal mine. Section 3.1 describes the near infrared spectroscopy of methane. The potential effects of other atmospheric constituents is presented in Section 3.2. In Section 3.3, the absorption band most appropriate to a room temperature diode laser DIAL measurement is found.

Chapter 4 describes in detail the operating characteristics of the high power diode lasers used on the present project. Section 4.1 explains their fabrication and physical form. Sections 4.2 through 4.4 delineate the laser output: spectral properties, polarization tendencies, and beam spatial characteristics, respectively. The polarization is found to be unusual. Results of experimental lasing threshold and efficiency measurements are presented in Section 4.5. The resulting patterns are contrasted to those of standard diode laser models. Section 4.6 discusses diode lifetimes. A brief explanation of the unusual properties found in Sections 4.3 and 4.5 is attempted in Section 4.7.

The requirements for a diode laser DIAL measurement of methane in a coal mine are presented in Chapter 5. Section 5.1 the applicable federal regulations. Laser safety considerations are discussed in Section 5.2. The detection restrictions
on the laser optical output power and pulse repetition frequency are derived with help from the appendices in Sections 5.3 and 5.4.

Chapter 6 develops the optical design for a dual diode laser external grating cavity methanometer source. A brief summary of the DIAL requirements and diode laser properties presented in earlier chapters is given in Section 6.1. Section 6.2 presents external resonator diodes lasers as a means of matching the DIAL requirements with the diode properties. Section 6.3 then discusses the use of reflective optics for an external grating diode laser cavity. Specifically, the application of aluminum off-axis paraboloids is presented as advantageous. In the chapter's last section, 6.4, The optical aberrations of such an off-axis cavity are discussed theoretically through analogy to monochromator theory and through application of a ray-tracing program.

Chapter 7 describes the construction and performance of a dual diode source. Section 7.1 explains the source mechanical construction. Section 7.2 lays out the antireflection coating process used to decouple the diode laser from its normal oscillating modes. In Section 7.3, the cavity electronic components are described. The last section, 7.4, shows the source performance.

The final chapter, Chapter 8, summarizes the preceding pages. In addition, that chapter attempts to point out new techniques using diode lasers that might be applied to remote sensing problems. Specifically, recent work on cleaved-coupled-cavity high optical power phased array diode lasers is discussed as a potential means to achieve the spectrally narrow output necessary for remote measurements of chemical species.
2. THE DIAL TECHNIQUE

To satisfy various state and federal regulations, present practice in room-and-pillar coal mines is to stop mining operations to measure methane levels at one foot from the working face. By law, the measurement must occur every 20 minutes. The measurement is made with a hand-held device either extended to the face on a telescoping pole or carried to the face after temporary roof supports are installed. The modern hand-held methane monitor is a far cry from the caged canaries once used to detect high levels of noxious gas, and more certainly, contemporary monitoring techniques are far superior to the ancient practice of sending the "fire-boss" through the mine before each working shift with a flaming torch to burn out any methane accumulations. The present monitoring technology does, however, hamper production and endanger miner safety leading to less than perfect compliance with regulations. Further, some types of gas detection instrumentation currently employed have been used since early in the last century with little or no improvements. The flame safety lamp, for example, has been used to measure methane since 1816. In the last fifteen years there have been several attempts to improve local coal and natural gas measurement methods, but until recently there have been no attempts at a truly remote measurement for mines.

A new direction in the process of improving mine methane monitoring was taken in 1978 when specifications for a remote methane measurement instrument
were drawn up at HRL. Researchers at HRL, after a thorough of study of available techniques, concluded that the LIDAR method could best be applied in the coal mine environment to remotely detect methane in coal gas.

2.1 LIDAR: Fluorescence, Raman Scattering, Absorption

The first uses of lasers for remote sensing were in radar type applications. Consequently, the acronym LIDAR for Light Detection and Ranging was applied to laser ranging systems. The first use of LIDAR, in 1963, located turbidity in the upper atmosphere. Soon thereafter LIDAR sensing techniques took on many new tasks, such as remote pollutant detection. There exist currently three different means of measuring from a single location remote gas concentrations with LIDAR: fluorescence, Raman backscatter, and long path or differential absorption. These three methods have been thoroughly reviewed.

All three techniques may be explained and compared by means of the fundamental LIDAR equation:

$$P_r(R) = \left( \frac{\rho}{\pi} \right) KP_0 \left( \frac{A}{R^2} \right) e^{-2\int_0^R \alpha(r)dr}$$  \hspace{1cm} (2.1)$$

where $P_r$ is the backscattered light signal from a target at range $R$, $P_0$ is the transmitted power, $K$ is the optical receiver system efficiency, $(\rho/\pi)$ is the effective reflectivity of the target, $A$ is the area of the receiving telescope, and $\alpha$ is the volume extinction coefficient of the atmosphere traversed by the transmitted and reflected light. Figure 2.1 shows schematically a typical single-ended LIDAR system. In the figure, light is transmitted to a remote location and is backscattered to
Figure 2.1  A monostatic LIDAR system.
the transceiver. In the case of fluorescence and Raman backscatter, the return signal is scattered by the species to be detected; which is to say, $\rho$ is proportional to the respective backscatter cross sections. When absorption methods are employed, atmospheric Rayleigh, Mie and/or localized retroreflectors scatter back the transmitted light.

Fluorescence techniques have little use at atmospheric pressures and temperatures. In the application of this method, transmitted laser light excites the remote species to be detected to a higher energy state and subsequently backscattered fluorescence is measured. However, at normal temperatures and pressures rotational state relaxation processes and quenching fluctuations preclude sufficient signal levels ($\rho$ small) and signal stability ($\rho$ not well known), respectively.

Conversely, Raman methods have enjoyed some experimental field success. In applications, short wavelength laser light is transmitted to a remote chemical species and the backscattered Stokes radiation is detected. This technique has been used, for example, to measure the temperature and pressure of atmospheric water vapor. Recent reviews of remote Raman methods may be found in the literature.

Indeed, Raman backscattering from methane is currently being pursued for potential coal mine applications by the USBM through its Pittsburg Research Center. In this scheme, 337.1 nm. light from a nitrogen laser is transmitted into a nitrogen and methane atmosphere. The Raman return signals are detected at 365.84 nm. and 373.82 nm., respectively. In practice, the ratio of the methane return signal to the nitrogen (assumed to be of known and constant concentration) return signal is used to calculate the methane density. This system, if employed in a mine, would have the advantage of easily being adapted to other potentially
hazardous gases by a simple replacement of filters in the receiving optics. Additionally, it is advantageous that the Raman technique relies only on the species to be detected for backscattering; consequently, no other backscatter source need be present to create a return signal. Moreover, it is beneficial that Raman LIDAR systems require only a single frequency transmitter, as opposed to a dual frequency source for absorption LIDAR setups.

There are, however, a number of problems that would be encountered by any attempted implementation of such a technique in coal mines. These technical concerns have been outlined previously. The principal probable problems are weak return signals ($P_r \approx 75$ photons/sec. for methane), potentially explosion inducing high voltages (20 kV in the nitrogen laser), and ultraviolet transmitted light levels near safety limits for eye exposures.

In the absorption mode, LIDAR systems transmit light alternately on and off an absorption wavelength characteristic of and particular to the species to be detected. The return signal from the light transmitted off the absorption line provides a measure of the attenuation due to Mie and Rayleigh scattering along the path. The return signal from light transmitted at the absorption wavelength includes the effect of absorption by the species of interest. The difference in the two signals then yields the effect of absorption alone. Thus, in this mode, a sensitive measure of species concentrations is possible. This is the same as to say $\alpha_{on}\!-\!\alpha_{off}$ from Equation 2.1 can be large; and consequently, $P_{r, on}\!-\!P_{r, off}$ can be significant. However, in order for $\rho$ to be large enough for a sufficient signal-to-noise ratio (SNR) at the receiver, it is often necessary for some retroreflector to be introduced into the absorption LIDAR path. Fortunately for the potential use of absorption
LIDAR in coal mines large amounts (10-200 mg/m³) of coal dust are present near a working face during mining operations. Thus, the location and timing mandated by statute for methane measurements in coal mines would seem to ensure a high value of $p$ in Equation 2.1. This large value of $p$ coupled with the intrinsic sensitivity led Byer to recommend absorption LIDAR to HRL in 1978 as a means to remotely measure coal gas methane.

Absorption LIDAR schemes may be divided into two categories: path averaged and range-resolved. The first category yields the integrated species concentration over the entire light path of Figure 2.1. In this mode, no information about the spatial distribution of the gas is available. The second category gives the desired gas density as a function of one or more spatial coordinates. This distribution may be derived from light time of flight measurements or optical triangulation. To meet the statutory requirement of measurement one foot from the working face, the geometric range resolved method was chosen at HRL in 1978 for experimental work in 1979.

2.2 Overview of Range Resolved DIAL

In the same year that LIDAR was first demonstrated, 1963, Schotland measured atmospheric water vapor using range resolved DIAL (RDIAL) and a temperature tuned ruby laser. (An early convention of reserving the acronym DIAL for range resolved absorption LIDAR is now largely ignored in the literature and so shall be here.) During the last decade numerous reports of DIAL experiments have appeared in the literature. The laser systems employed have included CO₂, argon-ion, IR optical parametric oscillator, dye, dye+SHG, and cryogenic...
cally cooled lead-salt diode lasers (also known as tunable-diode-lasers or TDLs) among others. Examples of DIAL review papers may also be found. Two papers in particular give a theoretical and experimental treatment of RDIAL.

As was mentioned in the last section, regulatory requirements necessitate the use of RDIAL for coal mine applications. The fundamental equation for RDIAL is given by Equation 2.1 with:

\[
\frac{\rho}{\pi} = \left( \frac{c \tau}{2} \right) \left( \frac{\beta}{4 \pi} \right)
\]

(2.2)

for temporal ranging and

\[
\frac{\rho}{\pi} = \left( \frac{\beta \Delta R}{4 \pi} \right)
\]

(2.3)

for spatially resolved ranging, where \( c \) is the speed of light, \( \tau \) is the laser light pulse duration, \( \beta \) is the backscatter coefficient at \( R \), and \( \Delta R \) is the geometrically determined sample depth as shown in Figure 2.2. The spatial resolution required for methane measurements in coal mines is approximately one foot since law requires measurement at one foot of the face. Thus in temporal ranging

\[
\frac{c \tau}{2} < 1 \text{ foot}
\]

(2.4)

is required. This requirement implies a laser pulse duration of less than 2 ns and is the ranging contemplated for the USBM Raman work described above. With a geometrically determined sample depth, there is no restriction on laser pulse duration; and consequently, smaller detector electronic bandwidths are possible. This latter ranging method was chosen by HRL for the 1979 experimental work mentioned previously. This latter technique is also the one that the 1981 OGC report.
Figure 2.2 A spatially range-resolved DIAL system.
considered for use with diode lasers.

Hence for the work described here, the basic RDIAL equation is given by:

$$P_r(R) = \left( \frac{\beta \Delta R}{4\pi} \right) KP_0 \left( \frac{A}{R^2} \right) e^{\int_0^R 2R \alpha(r) dr}.$$  \hspace{1cm} (2.5)

In this equation

$$\alpha = \alpha_R + \alpha_{\text{MIE}} + \alpha_{\text{ABS}}$$ \hspace{1cm} (2.6)

where $\alpha_R$ and $\alpha_{\text{MIE}}$ are the Rayleigh and Mie scattering coefficients of the coal mine atmosphere and $\alpha_{\text{ABS}} = N \sigma_{\text{ABS}}$ is the molecular absorption coefficient due to a molecular density $N$ with an absorption cross-section $\sigma_{\text{ABS}}$.

In practice, Equation 2.5 must be inverted to solve for $N$. This will be discussed in detail in Chapter 5 and in the appendices.

2.3 Prior Uses of DIAL to Remotely Measure Methane

Methane is released into the atmosphere by numerous sources. It leaks from natural gas delivery lines, garbage dumps, and water-logged soils. Autos and coal mines spew it. It evolves from animal feces. The global atmospheric concentration is about 1.5 ppmv and is increasing at a rate of 1-2% per year\textsuperscript{51}.

The many sources of atmospheric methane have generated considerable interest in attempts to remotely detect the gas. There have been several reports during last decade of successful detection by DIAL methods. The overlap of methane absorption lines with He-Ne and Er:YAG emissions was noted in 1965 and 1972, respectively\textsuperscript{52, 53}. Soon thereafter LIDAR techniques were applied. Murray and co-workers at Stanford Research Institute (SRI) used a DF laser and long-path
techniques to demonstrate measurement at 3.7 μm. Baumgartner and Byer used a tunable IR optical parametric oscillator to detect methane in the open atmosphere at 3.39 and 1.66 μm. Grant and others at the Jet Propulsion Laboratory have developed He-Ne systems for use along gas delivery pipe lines and at garbage dumps. Rosengreen and Altpeter have reported on upconversion of CO₂ light in AgGaS₂ and AgGaSe₂ for detection of CH₄ in the 3 to 3.5 μm range. Recently, Chan et al. reported using InGaAsP LEDs to measure absorption in methane at 1.33 μm and 1.66 μm by a method analogous to DIAL.

In 1975, White and Watkins proposed the Er:YAG laser as a remote sensor of methane. Later they conducted long-path absorption experiments with the same device. In 1979, Egan, DeFreez, Boos, and Byer demonstrated the first geometrically range resolved DIAL measurement of methane. In their experiments, Er:YAG laser light was Mie backscattered from remotely situated coal dust suspended in a methane and air mixture simulating a working coal mine face. Recently, a transportable Er:YAG RDIAL-MIE backscatter methanometer, built for Bethlehem Steel Corporation (BSC) following the 1979 design, has been successfully demonstrated at a USBM above ground mine simulator and in a BSC underground working coal mine. The goal of the present project has been to design and build a dual wavelength diode laser light source capable of replacing the Er:YAG source in that methanometer.
3. SPECTROSCOPIC CONSIDERATIONS

One of the first tasks in the present study was to determine which line or lines of the methane absorption spectrum were most suitable for a diode laser RDIAL methanometer. That determination had to be based on the absorption characteristics of the various methane lines, and on the compatibility of the line wavelengths with the technology of diode lasers. Further, it needed to be based on the absorption characteristics of any other relatively abundant naturally occurring atmospheric constituent or any abundant coal gas component.

Three criteria determine the suitability of absorption lines for a diode laser RDIAL methanometer. First, the line or lines must be within the spectral region accessible to high power diode lasers exhibiting reasonable efficiency and lifetime at or near room temperature. This requirement restricts consideration to injection diode lasers in the near IR. Second, the line or lines must be of appropriate absorption strength, so that the RDIAL measurement process is not impaired either by lack of sensitivity or by excessive attenuation. Based on the experimental work performed at HRL in 1979, an appropriate absorption strength, S, was determined to be between $10^{-22}$ to $10^{-21}$ cm/molecule. For a source of better understanding of the somewhat obtuse unit cm/molecule see reference (71). S is proportional to the absorption cross-section per molecule at the absorption line center times the line width. Thus S has units of $\frac{\text{cm}^2}{\text{molecule}} \times \text{cm}^{-1}$. Third, the absorption line or lines
must have an effective overlap with other coal mine atmospheric constituents of much less than $10^{-22}$ cm/molecule. For this criterion, it was assumed that interference from sources other than coal gas, such as diesel exhaust, could be ignored\textsuperscript{20}.

The first criterion above limits the spectral region that needs to be examined to the range from 2500 to 12,500 cm\(^{-1}\) (i.e. wavelengths from 4 µm down to 800 nm)\textsuperscript{70}. Further, the room temperature condition mentioned above highly favors the shorter wavelength portion of this region\textsuperscript{72}. Hence the near infrared (NIR) spectral region holds the most promise for a diode laser RDIAL methanometer.

\section*{3.1 The Near Infrared Spectroscopy of Methane}

Methane is second only to H\(_2\) in abundance among polyatomic molecules in the solar system\textsuperscript{73}. Yet its spectroscopy, particularly in the near infrared, is not well known\textsuperscript{74}.

In 1980, as part of the present project, the most comprehensive source of methane absorption parameters, the 1978 AFCRL Atmospheric Absorption Line Parameters Compilation\textsuperscript{71,75}, was explored. The compilation was stored on the HRL IBM-370 computer and its NIR region was interrogated by telephone-linked computer analysis from OGC. The analysis yielded three methane absorption regions of potential interest. A total of 1741 absorption lines were identified within these three bands and tabulated below in Table 3.1. In the table, the band assignment was given following the notation of Herzberg\textsuperscript{76}.

As has been pointed out, the near infrared spectrum of methane is not well known. Although the AFCRL compilation is the most definitive information available, its contents are lacking. For example, there are many absorption lines
between 5000 and 6000 cm\(^{-1}\) not due to \(2\nu_3\) and not found in the compilation. This is because no systematic absorption measurements have been made in the 1.6-2.0 \(\mu\)m range\(^{74}\). As recently as 1983, the \(\nu_2+2\nu_3\) band at 1.33 \(\mu\)m was measured\(^{77}\) apparently for the first time since it was originally characterized in 1933\(^{78}\). This band was then used for DIAL-like remote methane measurements using optical fibers and InGaAsP LED's\(^{62}\). Maximum absorption coefficients of 0.03 cm\(^{-1}\)atm\(^{-1}\) at 0.05 nm resolution to 0.054 cm\(^{-1}\)atm\(^{-1}\) at 0.3 nm resolution are obtainable at this wavelength depending upon which of the two articles cited \(^{77,62}\) above is believed. These coefficients are weaker than the absorption obtainable in band III, as will be shown in Section 3.3 with the help of the AFCRL data, and as has been noted \(^{79}\) recently by Chan et al. Also, Fox recently suggested\(^{80}\) that laser light absorption in CH\(_4\) near the 1.645 \(\mu\)m wavelength\(^{68,65,63,53}\) may be due to \(^{13}\)CH\(_4\) not \(^{12}\)CH\(_4\) as previously suggested\(^{53,81}\).

Absorption lines with a strength in the range mentioned in the second DIAL criterion above occur in all three bands noted in Table 3.1. However, band I is undesirable because of the requirement of room temperature laser operation. Further, not all bands are equally desirable in other respects, such as the possibility
of interference from other atmospheric constituents.

3.2 Effects of Other Atmospheric Ingredients on Band Selection

In addition to the problem that no diode lasers operate in band I at ambient temperatures, the band has other major drawbacks. For example, it encompasses nearly 3100 H₂O vapor absorption lines, some with strengths up to 2 x 10⁻²¹ cm/molecule. Room temperature air at 100% humidity has an H₂O molecular concentration of some 6 x 10¹⁷ cm⁻³. Thus it appears that water vapor alone is enough to preclude band I from use, since the present need is for methane detection down to a concentration of some 3 x 10¹⁵ cm⁻³.

Table 3.2 below shows naturally occurring components of air. Table 3.3 shows the constituents of coal gas. Of the table constituents, the AFCRL atmospheric absorption tapes show only H₂O and CO as methane's competitors in band II. CO competition is negligible for the distance range of the present application, since this species does not normally exceed 1 ppm in either the atmosphere or in coal gas.

While some H₂O lines in band II have a strength approaching 10⁻²¹ cm/molecule, these have a spectral density smaller than the more intense lines of band I. Also it is possible to find a few methane lines in regions where they are surrounded by water vapor lines of strengths not exceeding 10⁻²⁶ cm/molecule. Consideration of the usual coal gas constituents poses only one other possible problem for band II: that of a conceivably significant abundance of ethane. However, C₂H₆ has no strong absorption spectra above 3200 cm⁻¹. Thus band II could be used if an appropriate diode laser were available.
### Table 3.2 Naturally Occurring Constituents of Air

<table>
<thead>
<tr>
<th>Constituent</th>
<th>Listed in AFCRL Tape</th>
<th>percent</th>
<th>ppm</th>
<th>Absorption NIR Bands I or II</th>
</tr>
</thead>
<tbody>
<tr>
<td>N$_2$</td>
<td>Yes</td>
<td>78.1</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>O$_2$</td>
<td>Yes</td>
<td>20.9</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>Yes</td>
<td>0.03</td>
<td></td>
<td>Yes</td>
</tr>
<tr>
<td>Ar</td>
<td></td>
<td>0.9</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>Ne</td>
<td></td>
<td>18</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>He</td>
<td></td>
<td>5</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>Kr</td>
<td></td>
<td>1</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>Xe</td>
<td></td>
<td>0.09</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>H$_2$</td>
<td></td>
<td>0.5</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>CO</td>
<td>Yes</td>
<td>0.08</td>
<td></td>
<td>Yes</td>
</tr>
<tr>
<td>CH$_4$</td>
<td>Yes</td>
<td>2</td>
<td></td>
<td>No</td>
</tr>
<tr>
<td>N$_2$O</td>
<td>Yes</td>
<td>0.3</td>
<td></td>
<td>Yes</td>
</tr>
<tr>
<td>H$_2$O</td>
<td>Yes</td>
<td>Varies</td>
<td>Varies</td>
<td>Yes</td>
</tr>
</tbody>
</table>

### Table 3.3 The Composition of Coal Gas

<table>
<thead>
<tr>
<th>Constituent</th>
<th>Listed in AFCRL Tape</th>
<th>Maximum Amount Present (Volume %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH$_4$</td>
<td>Yes</td>
<td>99</td>
</tr>
<tr>
<td>C$_2$H$_6$</td>
<td></td>
<td>1.6</td>
</tr>
<tr>
<td>C$_3$H$_8$</td>
<td></td>
<td>0.05</td>
</tr>
<tr>
<td>C$<em>4$H$</em>{10}$</td>
<td></td>
<td>0.02</td>
</tr>
<tr>
<td>C$<em>5$H$</em>{12}$</td>
<td></td>
<td>&lt; 1 ppm</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>Yes</td>
<td>14.8</td>
</tr>
<tr>
<td>O$_2$</td>
<td>Yes</td>
<td>0.5</td>
</tr>
<tr>
<td>N$_2$</td>
<td></td>
<td>36</td>
</tr>
<tr>
<td>H$_2$</td>
<td></td>
<td>0.02</td>
</tr>
<tr>
<td>He</td>
<td></td>
<td>0.05</td>
</tr>
</tbody>
</table>
It may be noted that until recently no semiconductor diode laser has been available in the spectral region corresponding to band II. However a review of the plots of band gaps and compatible lattice constants in the III-V compound family (see, for example, Thompson (70) or Kobayashi and Horikoshi (86) ) shows that GaSb or InAs could be a binary substrate for lattice matching to AlInAsSb, InGaAsP or InAsPSb quaternary alloys with a bandgap appropriate for band II. A group at the State Rare Metal Research Institute in Moscow has reported work with $\text{Al}_x\text{Ga}_{1-x}\text{As}_y\text{Sb}_{1-y}$ lasers that are matched to GaSb substrates\textsuperscript{87}, but these particular devices provide wavelengths no longer than 1.8 $\mu$m. Also, some work on DH InGaAsSb lasers with an emission wavelength near 2$\mu$m has been reported\textsuperscript{88}. To this point, work in the United States has concentrated on shorter wavelengths, although reduced Rayleigh scattering in optical fibers may drive future research to longer wavelengths.

Band III is one of the better known methane NIR absorption bands\textsuperscript{73,89,90}. The search of the AFCRL data revealed some 150 band III absorption lines of appropriate absorption strength. Competition in this band is provided only by a scattering of H$_2$O and CO$_2$ lines, none of which has strength appreciably exceeding $10^{-24}$ cm/molecule. Thus band III has desirable spectroscopic properties for a RDIAL methanometer.

3.3 Band Selection

Selection of band III for further study was based on the absorption characteristics described in the previous section and the technology of diode lasers. At the time of the selection several groups had reported epitaxial growth of room tempera-
ture injection diode lasers in the wavelength range of 1.6 to 1.7 μm\textsuperscript{12,15,14,16}. The devices were made with ternary or quaternary alloys in the In\textsubscript{x}Ga\textsubscript{1-x}As\textsubscript{y}P\textsubscript{1-y} system lattice matched to InP. It however remained to be seen whether DIAL measurements of band III methane lines were compatible with the performance characteristics of this type of diode laser.

First it was necessary to examine the methane absorption lines of band III in greater detail. The emission of a moderate to high power pulsed diode laser typically has a full width half maximum (FWHM) spectral bandwidth of several wavenumbers\textsuperscript{70}. So, computer-calculated light transmittance curves were generated for the P, Q, and R branches of the 2ν\textsubscript{3} methane absorption band, assuming a 2 cm\textsuperscript{-1} laser bandwidth. A copy of the source program used in generating the curves may be found in Appendix A.

The P, Q, and R branches correspond to the spectral sub-regions 5890-5995, 5998-6005, and 6010-6107 cm\textsuperscript{-1} respectively. The necessary line absorption strength information was digitally filed from the AFCRL tape at increments of 0.1 cm\textsuperscript{-1} between 5890 cm\textsuperscript{-1} and 6107 cm\textsuperscript{-1}. Transmittance curves were then generated around local transmission minima (i.e. absorption maxima) for a supposed CH\textsubscript{4} concentration path length product of 3.2 x 10\textsuperscript{19} molecules/cm\textsuperscript{2}. That number was chosen to model a potential coal mine DIAL measurement situation: 0.1% CH\textsubscript{4} assumed over a 40 ft. path with 2% CH\textsubscript{4} postulated for the 1 foot of path nearest the working face.

Figures 3.1 through 3.3 show the local minima in the transmittance curves so generated for the P, Q, and R branches of the 2ν\textsubscript{3} band. It may be seen from the figures that no minimum falls below 95% in the entire range. Even though it is
Figure 3.1  Transmittance through 1.2 cm-atm of CH$_4$ in the $P$ branch of $2\nu_3$ at a spectral bandwidth of 2 cm$^{-1}$. 
Figure 3.2  Transmittance through 1.2 cm-atm of CH$_4$ in the Q branch of $2
u_3$ at a spectral bandwidth of 2cm$^{-1}$. 
Figure 3.3  Transmittance through 1.2 cm-atm of CH$_4$ in the R branch of 2$\nu_3$ at a spectral bandwidth of 2 cm$^{-1}$. 
necessary to know the noise limitations of a proposed DIAL detection system, to determine the optimum absorption cross-section, it is apparent from Figures 3.1 through 3.3 that this cross-section is too small if a 0.1% methane concentration is to be detectable.

Curves were subsequently generated for similar parameters except for the substitution of a 1 cm⁻¹ laser bandwidth (Figures 3.4 through 3.6) and a 0.2 cm⁻¹ bandwidth (Figures 3.7 through 3.9). Chan et al. have recently measured the absorption spectra of the 2ν₃ methane band at a resolution of 1.1 cm⁻¹. The relative absorption strengths that they measured agree with Figures 3.4 through 3.6 in most respects. The most notable exception is their finding of anomalously large absorption for lines R8, and R9. Byer previously measured the R branch of 2ν₃ at a resolution near 2 cm⁻¹ and found a much smaller relative strength for these two lines. (It should be noted that the AFCRL tapes used for Figures 3.1 through 3.9 may be in error for line R6 as it appears that duplicate fine structure lines were included at 6076.954 cm⁻¹ thus causing a somewhat overly large absorption to appear there.) It is interesting to compare the absolute absorption strengths represented in Figures 3.3 and 3.6 with the measured values of references (79) and (90). Chan et al. found the absorption coefficient of R7 to be 0.07 cm⁻¹atm⁻¹ at a spectral resolution of about 1 cm⁻¹. From Figure 3.6 a coefficient of 0.038 cm⁻¹atm⁻¹ may be calculated for the same line. This ratio between the measured and calculated values is also typical to that of most of the other 2ν₃ lines. This may be so because the calculated values include the effects of pressure broadening at atmospheric pressure while Chan et al. measured absorption strengths at 60 torr. Byer measured an absorption strength of 0.01 cm⁻¹atm⁻¹ at a resolution of nearly 2 cm⁻¹ for R7 with 50 torr of methane buffered to atmospheric pressure in N₂. On
Figure 3.4 Transmittance through 1.2 cm-atm of CH$_4$ in the P branch of $2\nu_3$ at a spectral bandwidth of 1 cm$^{-1}$.
Figure 3.5  Transmittance through 1.2 cm-atm of CH$_4$ in the Q branch of $2\nu_3$ at a spectral bandwidth of 1cm$^{-1}$. 
Figure 3.6 Transmittance through 1.2 cm-atm of CH$_4$ in the R branch of $2
\nu_3$ at a spectral bandwidth of 1 cm$^{-1}$. 
the other hand, Figure 3.3 yields a strength of 0.02 cm\(^{-1}\) atm\(^{-1}\) at the same resolution. Thus, the absorption shown in Figures 3.1 to 3.6, although not agreeing exactly with measured values, gives a reasonable estimate of the usefulness of the \(2\nu_3\) band at those spectral bandwidths for the DIAL process. While Figures 3.4 through 3.6 show narrowing of the spectral bandwidth to 1 cm\(^{-1}\) offers little improvement in absorption over that of 2 cm\(^{-1}\) bandwidth, it can be seen from Figures 3.7 to 3.9 that further reduction in bandwidth would be useful.

Figures 3.7 through 3.9 show that a source with a 0.2 cm\(^{-1}\) (FWHM) bandwidth would have a transmission of only some 85\% when tuned on to one of the more powerful CH\(_4\) absorption lines. The peak absorption seen in Figure 3.9 on the R4 line corresponds to an absorption coefficient of approximately 0.15 cm\(^{-1}\) atm\(^{-1}\). This is three to five times the absorption found at 1.3 \(\mu\)m as mentioned in Section 3.1. This absorption strength would offer large light transmission (85\%) over 40 feet and reasonable discrimination (15\%) over the 1 foot nearest the working face.

It should be noted here that for Equation 2.5 to be valid the DIAL laser source bandwidth must be equal to or less than the absorption line width\(^{91}\). For methane lines broadened in atmospheric pressure air the linewidth\(^{84,92,93,94}\) is approximately 0.2 cm\(^{-1}\). Thus to use Equation 2.5 without situation dependent correction factors\(^{91}\) the source bandwidth must be less than equal to 0.2 cm\(^{-1}\).

On the other hand, further reduction in the source bandwidth could lead to difficulties. If the laser line were narrower than the absorption line and tuned to its center the intensity of the returned light signal could be low due to absorption over the 40 foot distance while tuning instabilities could result if the laser were to be
Figure 3.7  Transmittance through 1.2 cm-atm of CH₄ in the P branch of 2ν₃ at a spectral bandwidth of 0.2 cm⁻¹.
Figure 3.8 Transmittance through 1.2 cm-atm of CH₄ in the Q branch of 2ν₃ at a spectral bandwidth of 0.2 cm⁻¹.
Figure 3.9  Transmittance through 1.2 cm-atm of CH₄ in the R branch of 2ν₃ at a spectral bandwidth of 0.2 cm⁻¹.
tuned to the edge of an absorption line due to the steepness of the line edges. Moreover, speckle noise would be promoted if the coherence length of the laser output became comparable to or less than that of the envisaged sample volume

\[
\text{coherence length} = \frac{1}{\text{bandwidth in wavenumbers}}
\]

Thus a spectral resolution of less than, say, 0.05 cm\(^{-1}\) would be a handicap.

As Figures 3.8 and 3.9 show, the Q and R branches of band III both offer methane lines of appropriate strength for a laser bandwidth of 0.2 cm\(^{-1}\) FWHM. However, the Q branch lines have typical separations of only 1 cm\(^{-1}\) or so, while those of the other two branches have line separations of about 10 cm\(^{-1}\). The Q branch line proximity could cause difficulties for tuning during the off-line segment of the DIAL process.

In summary, the spectroscopy of methane has been examined to study the applicability of injection diode lasers in a DIAL detection process. The \(2\nu_3\) band has been found to be spectroscopically suitable with the Q and R branches therein showing the most favorable absorption strengths. This observation then leads to examination in detail of injection semiconductor laser properties at the band III wavelength in the next chapter. In particular, the diode lasers used for this project are discussed.
4. **InGaAs/InP INJECTION LASERS**

The last chapter demonstrated the $2\nu_3$ absorption band of methane ($\lambda \approx 1.65 \, \mu m$) to be spectroscopically suitable for a coal mine RDIAL methanometer. The spectral overlap of that band with the light output of $\text{In}_x\text{Ga}_{1-x}\text{As}_y\text{P}_{1-y}/\text{InP}$ injection lasers for particular values of $x$ and $y$ was noted. The present chapter describes the room-temperature properties of such injection lasers operating in $2\nu_3$ band. In particular, the attributes of the diode lasers used in this project are delineated.

There has been considerable interest in recent years in double-heterostructure (DH) semiconductor lasers having an output wavelength longer than that of GaAs ($\lambda \approx 0.9 \, \mu m$). In all room-temperature injection devices, these lasers have been formed of III-V compound materials. Usually, these have used a quaternary $\text{In}_x\text{Ga}_{1-x}\text{As}_y\text{P}_{1-y}$ light emitting layer with $x$ and $y$ chosen to match the $a_0 = 5.87$ Angstrom lattice constant of InP. The wavelength range thus possible is interesting for room-temperature sources, for detectors, and for fiber optic communication with minimum loss and/or dispersion, in addition to other applications.

$\text{In}_x\text{Ga}_{1-x}\text{As}_y\text{P}_{1-y}$ lattice matched to InP has a room-temperature long-wavelength limit of $\lambda \approx 1.65 \, \mu m$ for the ternary composition $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$. This
alloy has been studied for a diversity of applications including both photocconduct-
tive\(^{104}\) and photovoltaic\(^ {106,102,107}\) types of optical detectors and microwave FET's\(^ {108}\). Additionally, room-temperature lasing has been obtained in InP/In\(_{0.53} \)Ga\(_{0.47}\)As/InP structures by three different techniques of layer deposition. The three methods are molecular beam epitaxy (MBE)\(^ {15}\), liquid phase epitaxy (LPE)\(^ {14}\), and vapor phase epitaxy (VPE)\(^ {97}\).

Remote measurements using NIR DIAL require pulsed and high peak power light sources owing to detector dark current limitations\(^ {32}\). In fact, in the next chapter it will be shown that \(P_o\) of Equation 2.5 should be greater than 100 mW for a successful RDIAL coal mine methanometer. In the realm of injection lasers, 100 mW of light output implies either broad area\(^ {70}\) or phased array devices\(^ {109,110}\). Only recently has there been a report\(^ {111}\) on the construction of InGaAsP phased array devices. Thus in the spring of 1981 efforts were started at OGC to locate sources and secure samples of broad area diode lasers capable of high light power pulsed operation in the 1.65 \(\mu\)m spectral region.

Only one of the numerous attempts to secure diode lasers was successful. During 1981 and 1982, B. I. Miller of A.T.T. Bell Labs, Holmdel graciously supplied In\(_{0.53} \)Ga\(_{0.47}\)As lasers to this project. These devices\(^ {15}\) have been used throughout the course of this project and their properties are described in the following sections. All the properties described represent experiments on several devices and some measurements were conducted on hundreds of lasers. Some of the material presented in the sections below was previously reported by DeFreez et al\(^ {18}\).
4.1 Laser Fabrication and Physical Form

The MBE process\textsuperscript{112,15} used to grow the lasers described here started with an n-type InP substrate of (100) orientation. On this substrate, a 1 \(\mu\)m thick \(n \approx 10^{18}\text{cm}^{-3}\) Ge-doped InP buffer and cladding layer was grown at a substrate temperature of 450 °C to provide a smoother foundation for the GaInAs active layer. The substrate temperature was raised to 510 °C for growth of a lattice-matched Ga\(_{0.47}\)In\(_{0.53}\)As layer and then lowered to 450 °C for growth of the \(\approx 5 \mu\)m thick top InP cladding layer. The latter layer was subsequently doped p-type by Cd diffusion with a duration intended to place a p-n junction at the InP/GaInAs interface.

Plating and sintering was used to create metallic contacts layers over both faces of the large-area sandwich, which was then ready for isolation into individual lasers. The end facets were created by (011) cleavage. The sides were partially string sawn and then broken to fashion separate lasers. The lengths of the lasers thus created varied from 300 to 650 \(\mu\)m. The widths varied from 130 to 175 \(\mu\)m. Figure 4.1 is a scanning electron microscope (SEM) micrograph of an individual laser.

Figure 4.2 is a SEM micrograph of part of an end facet. The figure shows one feature common to all such micrographs taken, one unusual feature, and rounded artifacts extraneous to the laser. As in all other SEM photos taken, the InGaAs active region is shown as a dark horizontal band of approximately 0.65 \(\mu\)m thickness. This is the thickness that was planned in the MBE deposition\textsuperscript{15}. Figure 4.2 also shows several diagonal dark lines. Only one other facet photographed showed showed such lines. These lines appear to be inclined at a 63° angle to the junction...
Figure 4.1  SEM micrograph of a broad area InGaAs/InP laser. The InP substrate, InP cladding layer, InGaAs active region, and top InP cladding layer are visible.
Figure 4.2  SEM micrograph of part of an InGaAs/InP laser facet. The two light areas are the InP cladding layers and the dark region is the InGaAs active region.
plane. When correction is made for viewing direction, the diagonals are found to lie along the intersection of the (111) planes with the end facet (011) plane.

It would thus appear that, in cleaving this facet, some jog planes were created as occasional interruptions of the (011) facet surface. Any such interruption that passes across the end of the active region can be expected to weaken the spatial coherence of the laser output and be a source of non-radiative carrier recombination. This latter circumstance could lead to catastrophic failure at high injection levels. Indeed, the reason this device was used for SEM viewing was its catastrophic failure at a high drive current.

4.2 Laser Output Spectral Characteristics

The spectral output for 15 of these lasers was measured at T~293 K with low duty cycle high current pulses. The pulse repetition frequency (PRF) was between 100 and 500 Hz resulting in a duty factor of <10^-4 using 150 ns pulses. Owing to the low duty cycle, average input power was low, but peak input power reached as high as 10 W. The drive current used for the spectral runs was from 1.5 to 3 times lasing threshold. The various lasers measured had threshold currents ranging from 1.7 to 4.7 Amps, which is equivalent to an area and thickness normalized threshold of 4 to 10 kA/cm^2μm.

The spectral response curves showed from 4 to 8 maxima in each case. As would be expected for the pulsed mode operation, the various spectral maxima represent multiple longitudinal mode operation\(^{113}\). Figure 4.3 shows the extreme case of 8 modes spanning the range 1.626 to 1.651 μm. The spectral width shown is greater than 20 nm. Of the various lasers measured while in contact with a room
Figure 4.3  Optical output vs. wavelength for a broad area InGaAs/InP laser. The laser is operated in a low duty cycle with a 150 nsec optical pulse.
temperature heat sink, none had modal wavelengths outside the limits of those in Figure 4.3. The spectral curves were obtained by synchronous detection of the output with a germanium photodiode and a Jarrell-Ash Mark X 0.275 m monochromator.

For one of this group of lasers, of length 420 μm, the modes were separated by 1.3 nm. However, for most spectral scans the modal separation was two or three times larger, indicating missing modes.

The minimum modal separation for a diode laser is related to its group index of refraction through the equation

$$\delta \lambda = \frac{\lambda^2}{\left(\mu_{\text{eff}} - \lambda \frac{d\mu_{\text{eff}}}{d\lambda}\right) 2L}$$

(4.1)

where $\lambda$ is the emission wavelength, $\delta \lambda$ is the modal separation, $L$ is the cavity length, $\mu_{\text{eff}}$ is the effective refractive index for light in the active region, and $\mu_{\text{eff}} - \lambda \frac{d\mu_{\text{eff}}}{d\lambda}$ is the group index of refraction. For $\delta \lambda = 1.3$ nm, the group index is 2.5. Using an effective refractive index of about 3.5\textsuperscript{114}, where equal TM and TE optical confinement in the active layer is assumed\textsuperscript{115}, yields $\frac{d\mu_{\text{eff}}}{d\lambda} = -0.6$ at the lasing wavelength. This experimental group index is less than the 4.5 index normally found in GaAs diode lasers\textsuperscript{70} and the only one, to this author's knowledge, reported for InGaAsP/InP lasers. It should be noted that if the minimum $\delta \lambda$ observed here also has missing modes, then the group index would be larger by some positive integer factor. Thus the group index could theoretically take on the values 2.5, 5.0, 7.5, etc.
4.3 Output Polarization

The active region of a DH injection laser, the laser type used on this project, is cladded with material of lower index of refraction than that of the active region itself. The low index cladding forms a dielectric waveguide\textsuperscript{116} for the laser light and thus increases operating efficiency\textsuperscript{117}. When the guided wave has its $E$ field in the plane of the waveguide, it is said to be a transverse electric (TE) mode\textsuperscript{117}. Conversely, when the guided wave has its $H$ field in the plane of the waveguide, it is called a transverse magnetic (TM) mode.

Most recent analyses of the properties of InP/InGaAsP/InP lasers have concentrated on the behavior to be expected with TE mode polarization\textsuperscript{119,114}. However, the lasers of this project were found to be TM polarized. Under the pulsed room-temperature operation described above, the ratio of TM to TE polarization is much greater than 1. No Attempt was made to determine the phase relationship between the TM and TE components of the light output. Figure 4.4 shows the ratio of TM to TE emission plotted versus drive current for one device. The figure was generated by passing the light from the diode laser through a rotating Nicol Prism and and plotting the ratio of the extrema of the AC current produced in a Ge photodiode versus laser drive current. In the figure, the onset of TM polarization coincides with the lasing threshold. Below threshold, the ratio is slightly greater than 1.

The semiconductor laser monograph literature\textsuperscript{120,70,117} has tended to treat only TE polarization for DH lasers, since this is the mode usually seen. That mode is usually dominant because of the higher facet reflectivity for TE modes\textsuperscript{121,119,122}. TM-mode dominance thus implies that the gain minus internal absorption losses for such modes is greater than for the TE modes by an amount sufficient to compensate
Figure 4.4 Optical output polarization ratio vs. drive current for a broad area InGaAs/InP laser. The laser is operated in a low duty cycle with a 150 nsec optical pulse.
for the higher reflection losses. In short, for the fundamental transverse mode (the only transverse mode observed, as explained in the next section)\textsuperscript{70}:

\begin{equation}
(g_{TM_0} - \alpha_{TM_0}) > (g_{TE_0} - \alpha_{TE_0}) + \left( \frac{1}{L} \ln \left( \frac{R_{TE_0}}{R_{TM_0}} \right) \right)\tag{4.2}
\end{equation}

where \( g \) is the gain, \( \alpha \) is the absorption coefficient, \( L \) is the laser length, and \( R \) is the geometric mean of the facet reflectivities. For the lasers in the present study, \( L \approx 400 \mu m \), \( R_{TM_0} \approx 0.26 \), \( R_{TE_0} \approx 0.38 \). These numbers are consistent with:

\begin{equation}
(g_{TM_0} - \alpha_{TM_0}) > (g_{TE_0} - \alpha_{TE_0}) + 10 \text{ cm}^{-1} \tag{4.3}
\end{equation}

The possible relations between the various gains and losses will be discussed further in Section 4.7.

4.4 Output Beam Spatial Characteristics

Far-field beam divergence measurements were made on 15 of the diodes. The divergence was measured perpendicular to the active region by rotation of the diode laser relative to a fixed Ge photodiode. In each case the far-field distribution appeared to be TM\(_0\), although the active layer is thick enough to support the TM\(_1\) mode as well\textsuperscript{116}. Numerical values for the FWHM angular divergence were calculated by least-squares fitting of the data to Gaussian functions, and were all in the range from 62° to 70°.

This large divergence is consistent with an active layer thickness in the range 500-700 nm, based on the work of Butler and Kressel\textsuperscript{123}, and others\textsuperscript{124-126,118}, and on the noted similarity of TE and TM mode behavior with respect to angular divergence\textsuperscript{117}. 
An output-beam imaging system, using an IR vidicon, monitor, and associated electronics and optics, was set up to examine the diode laser near field spatial distribution. Figure 4.5 shows one example of the results obtained. The figure was formed by reproduction of a photograph taken directly from the television monitor. The horizontal streaking is an artifact of the television raster. Note that this laser has a filamentary output, with four dominant areas of lasing activity. Such filamentary lasing is often characteristic of broad area lasers because of mode self-focusing. The brighter filaments correspond to regions of smallest threshold current density, since observations while the current pulse amplitude was progressively reduced showed the lasing output more and more confined to the brightest of these regions.

4.5 Laser Threshold, Output, and Efficiency

InGaAsP/InP lasers with various structures have been developed in recent years. Usually these devices exhibit a larger temperature dependence of threshold current, $I_{th}$, and external differential quantum efficiency, $\eta_{ext}$, than do similarly fabricated GaAs lasers. This general characteristic of InGaAsP lasers degrades their operating performance at room temperature and above.

Several models have been proposed to explain the temperature dependence of $I_{th}$ and $\eta_{ext}$. The proposed models include Auger recombination, free-carrier losses, carrier leakage over the InP cladding layer barriers, and intervalence band absorption.

Some of the proposed models have been subsequently shown to be of little significance. By changing internal losses through varying facet reflectivity and
Figure 4.5  Near field spatial distribution of optical intensity of a broad area InGaAs/InP laser. The laser is operated in a low duty cycle with a 150 nsec optical pulse.
operating temperature, Higuchi et al. demonstrated intervalence band absorption to be unimportant. Chiu et al. have shown Auger enhanced field and hot carrier leakage to be the prime source of the temperature dependence of \( I_{th} \) and \( \eta_{ext} \). Their work showed that the temperature dependence was primarily due to the p doping level in the InP cladding layer a conclusion supported by other recent work.

Tamari et al. have constructed stripe geometry lasers of high efficiency \( (\eta_{ext} = 74\%) \) with no temperature dependence between 20 °C and 70 °C, contrary to previous results.

Some of the data from the present project is presented below and is interpreted in terms of the Auger theory. Data on output power versus drive current were obtained for 84 lasers. Figure 4.6 shows point by point data for three of the devices. These include sample 11, which had the largest threshold current, and sample 13, which had one of the smallest threshold currents in the group.

The subthreshold data in Figure 4.6 for sample 11 show a markedly sublinear (i.e., concave down) behavior. Sublinearity in this region is also vestigially apparent for sample 4. Dutta and Nelson have shown Auger recombination to be the source of this type of operating characteristic, since radiative recombination increases as \( n^2 \) while Auger recombination grows as \( n^x \) where \( x \) is between 2 and 3 and where \( n \) is the injected carrier density. This result has been corroborated by the other work.

However, \( I_{th} \) and \( \eta_D \) are less than ideal even for those lasers not exhibiting Auger characteristics. For example, the threshold current \( I_{th} \approx 1.8 \, A \) for sample 13, as illustrated in Figure 4.6, is equivalent to a threshold current density \( J_{th} \approx 2.8 \)
Figure 4.6 Optical output vs. drive current for three broad area InGaAs/InP lasers.
kA/cm². This is about 40% larger than the lowest threshold density given by the model of Botez\textsuperscript{118} for an active layer thickness of d≈600 nm. For some of the measured devices, J\textsubscript{th} was as much as 2.5 times greater again.

The external differential quantum efficiency was calculated from the slope above threshold of output power versus drive current for 84 lasers. Whereas Figure 4.6 expresses an ordinate in arbitrary units, these data were taken using a calibrated Ge photodiode. Thus, the absolute slope of light output versus drive current could be measured. Often 100 mW or more of light power, single facet, was observed at drive currents less than 3 times I\textsubscript{th}. Values for \( \eta_{\text{ext}} \) were found to lie in the range 0.030<\( \eta_{\text{ext}} \)<0.116 (double facet). All values in this range are far less than those recently reported for broad area InGaAsP devices\textsuperscript{136}.

It is a normal practice to deduce the internal quantum efficiency (\( \eta_i \)) and the effective internal absorption coefficient (\( \alpha_i \)) by using the equation\textsuperscript{70}:

\[
\eta_D = \frac{\eta_i}{1 + \alpha_i L / \ln(1/R)}
\]  

(4.4)

where \( L \) is the cavity length, and \( R \) is the geometric mean of the end facet reflectivities, and \( \eta_D \) is the abbreviated expression for the external differential quantum efficiency. From Equation 4.4, a plot of (1/\( \eta_D \)) should yield a straight line with positive slope proportional to \( \alpha_i \) and with intercept 1/\( \eta_i \). However, when 1/\( \eta_D \) for the sample of 84 lasers was plotted against length, in Figure 4.7, a minimum occurred near \( L=400 \mu m \) with the slope of the curve being negative below this value. The negative slope implies a negative, nonphysical, absorption coefficient in Equation 4.4, which leads to the discussion in Section 4.7.
4.6 Laser Lifetimes

There has been interest recently in the operating lifetimes of InGaAsP/InP injection lasers. It has been noted that the InGaAsP devices have a potentially longer operating life than their AlGaAs counterparts.\(^{70}\)

The InGaAsP potential for long lifetimes is caused by a number of factors. The dark line defects common to AlGaAs devices have been found to be scarce in InGaAsP structures at both room temperature and elevated temperatures. Long term facet oxidation has been found to be a source of degradation in InGaAsP lasers. However, the degradation rate is about two orders of magnitude smaller than for AlGaAs lasers when operated at room temperature with an optical output of \(\approx 1\) MW/cm\(^2\). In fact, the change in the threshold current for InGaAsP diodes has been measured to be less than 1\% when operated for 1000 hours in a CW mode at room temperature.\(^{140}\) Also, catastrophic dark line defects, common to AlGaAs laser facets, are not generated in InGaAsP devices below 100 MW/cm\(^2\) of light output.\(^{141}\) The diodes of the present project operating at 100 mW of output power, have a power density of \(\approx 0.1\) MW/cm\(^2\).

During this project, no long term laser degradation has been observed for the drive currents and output powers used. A life test was conducted on one sample. It was pulsed at 6 Amps and 400 Hz PRF with 160 ns pulses. The diode was observed to stay within \(\pm 15\%\) of its average output for \(10^8\) sequential pulses, with no sign of any downward trend. The diode was then pulsed at 9 Amps, resulting in a 60\% increase in the output power. After operation for \(10^9\) more pulses there was no apparent degradation. Additionally, many devices have been run intermittently over much longer periods, weeks to months, at a 10 kHz prf with no sign of degrada-
Figure 4.7 Reciprocal external differential quantum efficiency vs. laser cavity length for 84 broad area InGaAs/lnP lasers.
tion.

However, during the project, several devices catastrophically failed at injection current densities of about 20 kAmps/cm². No attempt was made to identify the mechanism associated with this failure mode although the failure symptom is facet damage. Figure 4.8 shows the facet of one such device. In the figure, the horizontal band, labeled "A", was caused by localized melting at high drive currents. In light of recent work reporting 100 MW/cm² thresholds¹⁴¹ for optically induced facet damage in the InGaAsP device family, it is likely that the observed melting is caused by nonradiative carrier recombination. Chapter 7, in its discussion of antireflection coatings for laser facets, presents further evidence for nonradiative carrier recombination.

4.7 Discussion

As outlined above, the experimental data provided two unexpected results. First, deduction of the internal absorption coefficient using the standard method (Equation 4.4) produced a nonphysical value. Second, while most DH injection lasers are TE polarized, all the devices measured were TM polarized.

Figure 4.7 shows a plot of the inverse external differential quantum efficiency \(1/\eta_D\) versus laser length for 84 lasers. The lasers were grouped according to length in 50 \(\mu\text{m}\) intervals. The error bars show the standard error in the mean. If the usual equation for \(\eta_D\) versus length were to hold here, a straight line plot would be expected. This is clearly not the case in the figure.

In this connection, Whiteaway and Thompson¹⁴² have described a different loss model for a DH laser not far above threshold. Not far above threshold means, here,
Figure 4.8 SEM micrograph of facet of InGaAs/InP laser after catastrophic failure.
operation at drive currents corresponding to that part of the light versus current curve above threshold but before any inflection. The model of Whiteaway and Thompson is consistent with \( \frac{1}{\eta_0} \) first decreasing with length and then increasing at larger lengths. This is consistent with the pattern observed in Figure 4.7.

Indeed, when the constants appropriate to TM mode reflectance losses and to the operational conditions used are inserted into the provisions of a slightly simplified Whiteaway and Thompson model, interesting families of curves can be plotted for \( \frac{(\eta_1/\eta_0)}{\eta_1} \) versus L. The families are generated with the internal absorption coefficient \( \alpha_i \) as a parameter. Such a family with \( \eta_0 = 0.4^{143} \) is plotted in 4.7. As the figure shows, the experimental points are consistent with an absorption coefficient \( \alpha_i \approx 20 \text{cm}^{-1} \). The discrepancy in the figure at shorter wavelengths must be caused by something other than the small statistical sample shown.

This chapter has explained in detail the properties of high power diode lasers that possess a spectral overlap with the CH\(_4\) \( 2\nu_3\) absorption band mentioned in Chapter 3. Chapter 5 examines the requirements for a diode laser DIAL methanometer for coal mines. Chapter 6 will then bring together these topics. That chapter introduces external resonator diode lasers as a means of matching the diode laser characteristics presented here to the DIAL requirements presented in the next chapter.
5. METHANOMETER REQUIREMENTS

Both statutory and technical considerations determine the design requirements for a diode laser DIAL methanometer for use in coal mines. The statutory criteria determine the accuracy, frequency, and safety requirements of methane measurements in underground mines. Technical considerations set, along with other parameters, the laser optical power and spectral bandwidth. This chapter presents the pertinent requirements and lays out the means by which a remote diode laser DIAL methanometer can meet them.

5.1 Federal Regulations

Federal regulations apply to remote measurements of methane in coal mines in two ways. First, federal law requires a methane measurement every twenty minutes at one foot from a working mine face. This same law specifies that mining must cease whenever the measured methane concentration exceeds 4%. As was mentioned in Chapter 2, this regulatory requirement necessitates the use of range resolved DIAL (RDIAL) techniques in the present context. The basic RDIAL expression, Equation 2.5, was derived in the same chapter. In this chapter, in Section 5.3, that equation will be inverted to solve for the methane concentration.
Second, federal law also specifies several particular requirements for portable methane detectors. In addition to general requirements about such matters as durability, practicality of operation, and serviceability underground that will not be discussed here, the law lays out specific performance requirements for indicating detectors. Indicating detectors are defined as devices "that will show, within certain limits of error, on an adequate scale, the percentage of methane in a gassy atmosphere" and are the devices appropriate to the present discussion. To be specific, an indicating detector must give indications (read measurements) as low as 0.25% methane and should give readings as high as 4% with a minimum upper capability of 2%. The indications for the various percentages must be within the limits of error shown in Table 5.1. The law further specifies that during tests of the instrument made at several percentages within the range of the detector neither the average of 10 readings nor more than 2 readings for each percentage may exceed the limits of error given in Table 5.1. Sections 5.3 and 5.4 will discuss the implications of the law on such system properties as optical output power and detector sensitivities. First, however, the maximum amount of safe laser emission near the 1.65 μm wavelength specified in Section 3.3 must be calculated.

5.2 Laser Power: Safety Considerations

An eye and skin safety calculation was carried out using the 1980 ANSI Standard and again using the Bureau of Radiological Health regulations. The two approaches yielded equivalent results and the explicit calculation using the ANSI Standard is presented in Appendix B. That calculation assumes a 100 ns pulse duration at a pulse repetition frequency of 10 kHz and gives an allowable peak opti-
cal power per pulse of 4.3 watts. The use of the pulse parameters given above is motivated by the lifetest data mentioned in Chapter 4 and the calculations of Sections 5.3 and 5.4.

The allowable peak optical power indicated by the safety calculation is much larger than that achieved to date with diode lasers operating with a narrow spectral output in pulsed mode. Thus safety is not a limiting factor for a diode laser DIAL methanometer. The required optical power is calculated in the next section.

### 5.3 Laser Power: Detection Considerations

An analysis of the optical output requirements must start with the fundamental RDIAL equation for the Mie backscattered signal (ie. Equation 2.5):

$$P_r(R) = \frac{\beta_{\text{Mie}} \Delta R}{4\pi} kP_0 \left(\frac{A}{R^2}\right) e^{-\int_0^R a(r)dr}$$  \hspace{1cm} (5.1)

where $P_r$ is the backscattered light signal from a target at range $R$, $P_0$ is the
transmitted power, \( K \) is the optical receiver system efficiency, \( \frac{\beta_{\text{Mie}}}{4\pi} \) is the effective reflectivity of the Mie scatter volumes, \( A \) is the area of the receiving telescope, and \( \alpha \) is the volume absorption coefficient of the atmosphere traversed by the transmitted and reflected light. Not all the above parameters are well known. In particular, \( \beta_{\text{Mie}} \) and \( \kappa \) can only be approximated. However, experiments conducted by this author at HRL in 1979 provide data relevant to the Mie backscatter coefficient of airborne coal dust.

In those experiments, \( \approx 2.5 \) watts of 1.65 \( \mu \)m radiation was directed onto a coal dust cloud with a concentration of approximately 40 mg/m\(^3\) and the backscattered portion was detected at a distance of 16 feet from the scattering volume. The returned optical power, \( P_r \), detector responsivity, \( R_D \), detected voltage, \( V_r \), and the amplifier gain, \( g \), follow the relationship:

\[
P_r = \frac{V_r}{gR_D}.
\] (5.2)

Since the experiments suggested \( V_r \approx 100 \) mv for \( g = 10^7 \) V/A and a detector responsivity \( R_D \approx 0.4 \) A/W, \( P_r \) must approximately equal \( 2.5 \times 10^{-8} \) watts. It should be noted here that there was no observed wavelength dependence of the returned signal on the wavelength tuning of the Er:YAG laser during these experiments. Thus, for the given distance and coal dust level

\[
P_r = 10^{-8} P_o.
\] (5.3)

Based on these results, the value of \( \beta_{\text{Mie}} \) is constant over a wavenumber range of few cm\(^{-1}\) range near 1.645 \( \mu \)m and is approximately 15 km\(^{-1}\), calculated from Equa-
tion 5.1 using the reasonable assumption of $\kappa \approx 0.1$. Recent experiments in a working mine\(^{67}\) show that the coal dust concentration at the active face may be as high as 100 to 200 mg/m\(^3\) and thus that $\beta_{\text{Mie}}$ may be as large as 75 km\(^{-1}\) at these dust levels. To further investigate the optical output requirements, an analysis of the various noise sources and their relative sizes must be made.

The signal-to-noise (S/N) power ratio of the returned signal in Equation 5.1 is given by\(^{148}\):

$$S/N = \frac{i_s^2}{i_{SN} + i_B^2 + i_D^2 + i_A^2} \quad (5.4)$$

where $i_s^2 = \text{the averaged squared signal current}$, $i_{SN} = \text{the averaged squared shot noise current}$, $i_B^2 = \text{the averaged squared background current}$, $i_D^2 = \text{the averaged squared detector dark current}$, $i_A^2 = \text{the averaged squared amplifier noise current}$. Standard expressions\(^{148}\) for the various currents and their calculated numerical values are provided in Appendix D.

It can be ascertained from that appendix that

$$i_{SN} : i_B^2 : i_D^2 : i_A^2 \approx 10^{-28} : 10^{-22} : 10^{-19} : 10^{-31} \Delta \nu. \quad (5.5)$$

It has been shown\(^{149}\) that $i_A^2$ can be reduced by orders of magnitude with current mode operational amplifiers so that noise source will not be considered further. It can also be seen from Equation 5.5 that $i_B^2$ is orders of magnitude less than $i_{SN}$ and thus may be ignored in the present context. To know more about the remaining two noise sources, $i_{SN}$ and $i_D^2$, a numerical value must be attached to $i_d$, the detector dark current.
The magnitude of the detector dark current depends on a number of device parameters and on the method of operation. When current mode operational amplification is used\textsuperscript{149}, the best detection sensitivity is achieved at zero detector bias or for small reverse voltages. It is known\textsuperscript{150} from load line analysis that linear operation is also achieved for near-zero bias. Thermally driven carrier generation-recombination is the source of dark noise near zero bias and its magnitude is given by

\[
\bar{i_D} = \frac{4 K_B T \Delta \nu}{R_D}
\]  \hspace{1cm} (5.6)

where \(R_D\) is the detector shunt resistance. Substitution of a typical value \(\approx 10^8 \, \Omega\) for a typical small area commercial Ge detector\textsuperscript{150} gives a value for \(\bar{i_D}\) some 60 times that of \(i_{SN}\), the quantum detection limit. Recently, extensive work has gone into the development and improvement of detectors for the 1.1 to 1.7 \(\mu m\) range. That work has been spurred by the growth of optical fiber technology, and the desire to operate fiber optic systems at wavelengths of minimum absorption and dispersion\textsuperscript{151,103}. In efforts to develop new germanium avalanche photodiodes, dark current densities near \(10^{-3}\) Amp/cm\(^2\) have been reported\textsuperscript{152,153} for room temperature large reverse bias operation. These current densities are slightly lower than those of the best commercially available devices and those of the HRL methanometer\textsuperscript{150}. However, these kinds of devices cannot be expected to show decreased noise at zero bias since the generation-recombination noise source is the same as that of previous germanium devices.

Alternative detectors to germanium have been in active development. They are based on the quarternary \(In_xGa_{1-x}As_yP_{1-y}\) system of direct-gap III-V semicon-
ductors. These can be lattice matched to GaAs for short wavelengths, and to InP for the longer wavelengths for fiber optics applications and for methane detection. This recent work on such detectors\textsuperscript{100,105,154-158,102,159,160} parallels the work, based on much of the same technology, of laser diode source development in that quarternary system.

In particular, Pearsall reported\textsuperscript{102} production of new InGaAs/InP photodiode structure with a dark current density of $3 \times 10^{-7}$ Amps/cm$^2$ at room temperature and a 1 volt reverse bias. The novelty of this device arises from physical separation of the photon absorption and depletion regions. Such a separation would not be possible below the direct bandgap threshold in a semiconductor such as germanium (ie. for $\lambda > 1.5 \mu m$). By placing the depletion region in the high bandgap ($\lambda \approx 0.9 \mu m$) InP portion, generation-recombination of carriers is minimized thus reducing the dark current and the generation-recombination noise associated with it. Thus a back biased dark current of 3 to 4 orders of magnitude smaller than in the best Ge devices is achieved. Pearsall also notes that the photon quantum efficiency is nearly 100% for $\lambda = 1.65 \mu m$ when the light is incident on the epitaxial side. That is a different situation from germanium for which the useful absorption decreases dramatically below the 1.5 $\mu m$ bandgap. Thus, with this type of detector, near shot noise limited operation is obtainable under the conditions described above and in Appendix D.

Due to the technical developments discussed above, high sensitivity back-side illuminated GaInAsP/InP detectors have recently been introduced to the commercial market. A typical such device\textsuperscript{161} has a sensitivity of -55 dBm at a $10^{-9}$ bit error rate (BER) and a bandwidth of 5 MHz. A BER of $10^{-9}$ is equivalent\textsuperscript{148} to a signal to noise ratio (SNR) of 11:1 and 5 MHz is the bandwidth appropriate to a 100
ns optical pulse. Thus, this detector can detect $3 \times 10^{-9}$ watts of optical power near 1.6 $\mu$m with a signal to noise ratio of 11:1. Using Equation 5.3, an optical output power of 100 mW would yield a SNR of 3.5:1 for a single pulse of light backscattered from 40 mg/m$^3$ of coal dust at a distance of 16 feet or 200 mg/m$^3$ at 35 feet.

Having obtained the value for the theoretically possible voltage SNR, the needed ratio for a DIAL measurement must be ascertained. This will be done in the next section.

5.4 SNR: Pulse Repetition Frequency Considerations

The federal requirements for a portable methane detector are shown in Table 5.1. It may be seen from the table that the allowed fractional errors in the measured methane concentration vary from $\pm 0.6$ at 0.25% CH$_4$ to $\pm 0.075$ at 4% CH$_4$. The law further requires for approval that a methane monitor must fall within the indicated errors in at least eight out of ten trials.

In Appendix C the inversion of the fundamental RDIAL expression, Equation 5.1 is derived. Equation C.17, therein, shows the completed inversion and is given by

$$
\mathcal{C} = \frac{C(r_2-r_1)}{2(R_1-R_2)} \ln \left( \frac{V_{\text{on}}(R_2)}{V_{\text{on}}(R_1)} \right) - \ln \left( \frac{V_{\text{off}}(R_2)}{V_{\text{off}}(R_1)} \right).
$$

in the notation of the appendix. That appendix in its second section also contains a detailed derivation of the error propagation inherent in the RDIAL measurement. A simple expression for the maximum allowable normalized standard deviation in
the measured voltages as a function of the required gas concentration and the amount of absorption in the sample volume during the on line portion of the RDIAL process is given in Equation C.28 and is given by

\[
\frac{\sigma_V}{V} = \frac{1}{2} \frac{\sigma_C}{C} \ln \left( \frac{V_{r,\text{on}}(R_2)}{V_{r,\text{on}}(R_1)} \right).
\] (5.8)

Substitution of \(\alpha C\) for the quantity inside the absolute value bars in Equation 5.8 yields

\[
\frac{\sigma_V}{V} = \frac{\sigma_C \alpha}{2}
\] (5.9)

where \(\alpha\) is the on-line absorption coefficient \(\approx 8.1\) from Section 3.3 for a 0.2 cm\(^{-1}\) source bandwidth. Evaluation of Equation 5.9 using the most restrictive condition on \(\sigma_C\) in Table 5.1 yields a required voltage SNR of 160:1.

Further consideration of the required SNR is required here in light of the statutory stipulation that an indicating methane monitor must satisfy the requirements laid out by Table 5.1 in only eight out of ten trials. Assume that the source of error in the methane measurement is random with a zero mean normal distribution. Then the probability of the measured CH\(_4\) concentration differing from the true value by more than two standard deviations is 4.54\%\(^162\). The requirement that eight out of ten measurements meet a specified accuracy suggests that the failure probability in the trials be calculated using a binomial distribution, with \(p = 0.0454\), \(q = 1 - p = 0.9546\), and \(n = 10\). It is easily shown by such a calculation that a SNR = 320:1 would pass the federal requirements nearly 99\% of any tests. Comparison of this SNR with the single pulse SNR of 3.5:1 derived above reveals the
need for a signal to noise improvement ratio (SNIR) of approximately 90:1. Signal averaging techniques can be used to improve the SNR.

One method of averaging often used with low duty cycle signals is the so-called boxcar method. Boxcar averaging yields a SNIR

\[ \text{SNIR} = \left( \frac{2N}{5} \right)^{1/2} \]  \hspace{1cm} (5.10)

where \( N \) is the number of pulses to be integrated. This method of integration is best used for large instantaneous signal low duty cycle averaging. Further enhancement to the SNIR beyond that of Equation 5.10 can be produced in this mode through preintegration techniques when sufficiently large instantaneous signals are available. However, in the present context the returned optical signal is not large relative to noise sources, so preintegration techniques are not feasible. Moreover, boxcar averaging is a nonlinear integration process that favors the last signals received and thus can introduce systematic errors in a non-stationary process. It will be seen below that the DIAL measurement process when averaged over many pulses is typically non-stationary. It will also be shown below that a SNIR greater than that of Equation 5.10 can be achieved by a digital signal processing method.

In recent years, there have been several investigations into the various sources of error in the DIAL measurement accuracy and into the signal processing techniques needed to minimize the errors. DIAL return signals are randomly affected by turbulence induced fluctuations in the absorber concentration, scintillation, beam wander, speckle, and the angle of arrival and by electronic noise. Additionally, differential reflectivity and differential background extinction are sources of systematic error in DIAL measurements.
It was shown in Chapter 3 that differential background extinction due to any of the normal constituents of air or coal gas is satisfactory for DIAL measurements in the wavelength region of the $2\nu_3$ overtone of methane. Furthermore, it was mentioned in Section 5.2 that the differential reflectivity from coal dust aerosols typical to coal mines was observed to not affect the backscattered light over a few wavenumber region near the 1.65 \( \mu m \) wavelength of an Er:YAG laser. So, the last two potential sources of systematic error are not a problem for a diode laser DIAL methane measurement at 1.65 \( \mu m \) in coal mines. The various sources of potential random signal errors must now be considered in turn.

The signal fluctuations caused by atmospheric turbulence and electronic noise may be classified by the degree of temporal correlation that they possess between on- and off-line portions of the DIAL process. Electronic noise between signal channels in a DIAL system is uncorrelated and may be reduced through averaging techniques by the factor $N^{-1/2}$ where $N$ is the number of samples averaged. Thus a SNIR of $N^{-1/2}$ is possible for signals affected by such noise.

Of the several atmospheric sources of potentially correlated noise, the latter four mentioned above should be minimal. Beam wander and angle of arrival variations would be negligible because of the short (~10m) path length for a coal mine measurement. Scintillation effects should also be negligible for a receiver aperture radius

$$R \geq (\lambda L)^{1/2} \quad (5.11)$$

where $\lambda$ is the laser wavelength and $L$ is DIAL total path length. $(\lambda L)^{1/2}$ is a transverse coherence length and is equal to approximately 4 mm for a 10 m path length and a wavelength of 1.65 \( \mu m \). Last, speckle effects should be nonexistent.
since the bandwidth gives, as shown in Section 3.3, a longitudinal coherence length less than the length of the scattering volume.

For periods of less than 1 to 10 milliseconds the atmosphere is "frozen". That is to say, for such periods the effects of turbulence on the two returned signals of a DIAL process are correlated. Thus, fluctuations of the returned signals because of methane concentration variations are correlated during this time interval.

It has been shown by Menyuk and Killinger that when the returned light pulses during the on- and off-line parts of the DIAL process arrive within the correlation time of the atmosphere subsequent signal averaging over many pulses diverges from the $N^{-1/2}$ improvement mentioned above for independent measurements. They found that the SNIR was less than $N^{-1/2}$ if the signals were averaged as

$$C = \text{constant} \times \ln \left( \frac{\langle V_{i,1} \rangle}{\langle V_{i,2} \rangle} \right)$$  \hspace{1cm} (5.12)$$

where $\langle \rangle$ represents time averaging. On the other hand, they found that the SNIR was greater than $N^{-1/2}$ for signals averaged as

$$C = \text{constant} \times \ln \left( \frac{\langle V_{i,1} \rangle}{V_{i,2}} \right)$$  \hspace{1cm} (5.13)$$

They attribute these properties to a high cross-correlation between the on- and off-line pairs and residual auto-correlation over many pulses because of the non-stationary nature of the absorber concentration. Menyuk et al. have recently presented a summary of the various parameters that influence DIAL measurement errors. Here it will be assumed that a SNIR of at least $N^{-1/2}$ can be achieved.
for a coal mine DIAL process with the latter signal processing method.

So, in a period of less than 1 second at a 10 kHz data collection rate a sufficient SNIR can be achieved to meet the SNR requirements derived earlier in this section provided the source properties presented in the last chapter can be modified to match those required by the derivations of this chapter. This is the next topic to be examined.
6. SOURCE OPTICAL DESIGN

This chapter brings together many of the previous topics. First, a review of the DIAL requirements and source properties is presented in Section 6.1. Next, in Section 6.2, external resonator diode lasers are introduced as a means of matching the diode laser characteristics to the DIAL requirements. In that section, the theory of linewidth narrowing in external grating cavities is discussed. Third, the advantages of reflective optics for an external cavity at a wavelength of 1.65 μm are presented in Section 6.3. In the last section, 6.4, the development and application of a ray-trace computer program to an off-axis parabolic mirror cavity is explained.

6.1 Review of Diode Source Characteristics and the DIAL Requirements

The properties of high optical power diode lasers as presented in Chapter 4 do not all match well with those source requirements developed in Chapters 3 and 5. This section presents, in review, the various characteristics discussed in those three chapters.

Most properties of broad area In$_{0.53}$Ga$_{0.47}$As/InP diode lasers are suitable for a coal mine RDIAL methane measurement. The achievable optical output power, $\approx 100$ mW, was shown to be sufficient in Chapter 5. The measured lifetimes at pulse
repetition frequencies of 10 kHz represent a potentially long period of service in a methanometer. The PRF possible is sufficient to obtain the necessary SNIR in less than one second. Also, the TM polarization characteristic described in Chapter 4, although not typical to most InGaAs/InP semiconductor lasers, is the polarization needed for operation in an external grating cavity.

Furthermore, the operating wavelength of In$_{0.53}$Ga$_{0.47}$As/InP lasers is near the $2\nu_3$ absorption band of methane. However, the typical spectral bandwidth at this wavelength, as shown in Figure 4.3 is much greater than the $\approx 0.05$ nm width required for sufficient absorption to make DIAL process feasible. Thus, a method is needed to control the bandwidth and wavelength while maintaining the other diode laser properties.

6.2 External Resonator Diode Lasers

No simple diode source can be made to satisfy, simultaneously all the requirements presented above. It is possible to achieve high optical power with broad active region or phase-locked array devices. However, this implies a broad spectral output as was shown, for example, in Chapter 4. Conversely, stripe geometry lasers yield a narrow spectral bandwidth but at low power. There are however means of solution of this circumstance.

All lasers consist of a gain medium and a resonator cavity for electromagnetic wave feedback. The cavity is physically defined by mirrors. For simple diode lasers the mirrors are cleaved facets parallel to the crystal planes of the as grown semiconductor. To modify the spectral, or any other, properties of a laser it is necessary to modify its internal characteristics (ie. the gain medium or resonator cavity).
External resonator diode lasers have been used for many purposes. The goals have been modification of the temporal\textsuperscript{177-182} and spectral\textsuperscript{183-192} properties normally observed. Numerous studies have been made of the intrinsic properties of diode lasers in external cavities or near reflecting surfaces, such as lens, optical fibres, or optical disks\textsuperscript{193-206}. The most recent review paper\textsuperscript{207} on diode lasers coupled to external resonators was published in 1979.

Almost all published accounts of continuous wavelength tuning and bandwidth control of diode lasers have reported on antireflection (AR) coated devices\textsuperscript{183-186,188,191} in external cavities. The few exceptions\textsuperscript{208,209} have involved low power single stripe devices in complicated temperature and current controlled servo-loops. By continuous wavelength tuning it is meant that the tuning resolution is much greater than the spectral separation of the diode laser modes. By AR coating the diode laser, its original facet reflectivity is nullified and thus the cavity can be extended to some external optical element. This allows access to the cavity and it is then possible to insert a wavelength controlling element such as an etalon, birefringent filter, or grating. In the present project an external 600 l/mm grating blazed for operation at $\approx 1.6 \mu m$ was substituted for one facet mirror after the facet was AR coated with a SiO coating. The grating, by selectively feeding back only a narrow spectral bandwidth of optical power to the active volume of the diode, forces the laser to oscillate in a limited spectral region. It be should noted here that in at least one previous case\textsuperscript{193} the facet reflectivity was nullified by lapping the facet at Brewster's angle with respect the active region. However, this method produces localized mechanical damage to the laser and severely degrades its lifetime.
It has been shown\textsuperscript{210,211} that a dielectric film with index of refraction given by

\begin{equation}
    n_f = \left( n_L n_{\text{ext}} \right)^{1/2}
\end{equation}

(6.1)

and thickness given by

\begin{equation}
    t = \frac{\lambda}{4n_f}
\end{equation}

(6.2)

where \(n_L\) is the effective index of refraction in the laser, \(n_{\text{ext}}\) is the external index, \(n_{\text{ext}} = 1\) for air, and \(\lambda\) is the vacuum wavelength of the laser radiation, gives a theoretical air-laser reflectivity of near zero. Thus by this coating technique a diode's emission may be decoupled from its normal oscillator modes and its spectral output may be controlled by substitution of a variable dispersion external cavity. This type of coating was used for this project. The results for a SiO coating are shown in Section 7.2.

Injection lasers exhibit homogeneous broadening\textsuperscript{212} and thus may collapse\textsuperscript{195} their wide filamentary lasing action into a narrow spectral region when they are employed in an external dispersive cavity. Furthermore this spectral narrowing may be done with little or no expense to the optical output power due to the homogeneous nature of the broadening.

The resulting bandwidth of an external grating cavity may be obtained from the standard grating equation as shown by Heckscher and Rossi\textsuperscript{186} and is given by

\begin{equation}
    \Delta \lambda = \frac{\lambda d}{2 f \tan(\theta)}
\end{equation}

(6.3)

where \(d\) is the active region thickness, \(f\) is the laser to grating collimating optics
focal length, and $\theta$ is the grating angle of incidence for a grating in a Littrow mount. This formula was derived using geometric optics. Substitution of numerical values appropriate to the present project, $\lambda = 1.65 \, \mu m$, $d = 0.65 \, \mu m$, $f = 25 \, mm$, and $\theta = 30$ degrees as calculated from the grating equation for a 600 l/mm grating, yields a bandwidth of $\Delta \lambda = 0.04 \, nm$. It is demonstrated in Chapter 7 that the bandwidth achieved during this project has never equaled that predicted by Equation 6.3. Therefore, it is important to ascertain if indeed this formula holds under a more sophisticated analysis of the spectral bandwidth.

A better estimate of the bandwidth to be expected from an external grating cavity can be achieved using coupled-mode theory of guided electromagnetic waves. Many recent developments in coupled mode theory have been driven by the interest in coupling the optical output of diode lasers to various types of waveguides, for example to optical fibres or thin films. Since a diode laser active region is itself a waveguide, it is appropriate to think of the coupling of the returned light from an external grating to the diode laser as a diode laser to waveguide problem. A revised estimate of the achievable spectral bandwidth is calculated in Appendix E using coupled-mode theory.

The derivation presented in Appendix E yields an expected bandwidth of 0.1 nm for a 2 times threshold drive current. This spectral width is 2.5 times that calculated by the generally accepted geometric optics method and is, as shown in Chapter 7, closer to that observed in experiments. It should be pointed out that this wider bandwidth reduces the absorption that may be achieved below that calculated in Chapter 3.

The degree to which an external grating can control the wavelength and bandwidth depends on the efficiency of the AR coating in suppressing residual modes.
of the diode laser cavity and on the reflective efficiency of the grating. It is known\textsuperscript{218} that a diffraction grating is effective only for light polarized perpendicular to its grooves. In a narrow bandwidth external grating diode laser cavity the grating grooves must be in the plane of the active region to ensure that the small dimension of the junction acts as a slit that rejects all but the desired part of the spectrally dispersed fed-back light. Because of this alignment, the fed-back light is then polarized perpendicularly to the active region plane, that is it is TM polarized. If the diode laser is intrinsically TM polarized, the returned optical power couples with the laser gain medium better than does TE polarized light. It was shown in Chapter 4 that the lasers used in the present project are TM polarized which is advantageous for use in an external grating cavity.

It was shown in Section 5.4 that a significant signal to noise improvement ratio (SNIR) could be achieved for the DIAL process when the on- and off-line portions of the process were temporally separated by less than the decorrelation time of the atmosphere, i.e. less than 1 to 10 ms. Double pulse DIAL systems have been used to take advantage of the improved SNIR. These systems have either used the combined output of two laser cavities operating at separate wavelengths\textsuperscript{219} or have used a movable wavelength control element in a single cavity\textsuperscript{220}. The former scheme suffers from duplication of all cavity components while the latter is necessarily slow because of mechanical inertia. For an external grating resonator diode laser system, a second diode laser may be placed adjacent to the first in the cavity. This second laser will be located at a slightly different angle to the grating relative to the angle of first laser and will oscillate at a different wavelength. So, the on- and off-line portions of the DIAL process could be initiated by alternate electrical drive pulses to the two diodes. This pulse scheme, with a 10 kHz interlace rate, was
implemented for this project and its mechanical and electronic construction are described in Chapter 7.

A final point about external resonator diode lasers: it is necessary to calculate the angular positioning stability required for the grating to maintain the wavelength of the light fed-back to the diode laser active volume within the bandwidth calculated in Appendix E. A simple trigonometric argument that ratios half the effective slit width to the focal length of the collimator optics gives that the angular stability must be given for small angles by

$$\Delta \theta < \frac{d}{2f}$$  \hspace{1cm} (6.4)

where the symbols are those defined following Equation 6.3. Numerical substitution yields $\Delta \theta < 25$ microradians.

Having explored external grating resonator diode lasers, it is now necessary to examine the means of optically coupling the diode laser and the grating. This is the topic of the next section.

6.3 Reflective Optics for an External Grating Cavity

Although exotic alternatives such as holographic optical elements are conceivable as the diode laser to grating coupler, common sense engineering suggests that refractive lenses or mirrors are more appropriate. Mirrors for use in the near infrared can be classified in turn into two categories: dielectric film and metal.

Work with refractive optics at the wavelength in question is both unusual and difficult. The difficulty arises from the low index of refraction of glasses, $n \approx 1.4$, at
1.65 μm wavelength. So, it is necessary when using glasses to have either more, or more powerful, optical elements to duplicate the effects achieved at visible wavelengths. During this project, several optical design and fabrication businesses were contacted regarding design and construction of a lens system to couple a 1.65 μm wavelength diode laser to a diffraction grating. Only one company, Research Optical Systems Group, Inc. (ROSG) was willing to bid on design and fabrication of such a device.

The pre-design plans from ROSG called for a five or six element glass lens system or a three or four element silicon lens system. The former would suffer from only 83-86% optical throughput because of reflection and scattering from the large number of optical surfaces involved and additionally would be bulky. The latter would be difficult to align since silicon is opaque to visible radiation. Implementation of either design would have been prohibitive due to engineering and tooling costs. The large number of problems associated with refractive optics made reflective optics more attractive for this project. Hence, it was decided to design a reflective laser-grating coupling system.

Since the coupling of the diode laser to a grating is from a finite conjugate point to an infinite conjugate, the mirror shape that would seem to give minimum optical aberration is parabolic. Furthermore, an unobstructed optical path from the diode laser to the grating requires an off-axis parabola. The focal length, f, needed to give adequate bandwidth, as discussed in the preceding section, along with the lateral dimension of the mirror needed to capture most of the rapidly diverging light emitted by the diode laser, see Section 4.4, necessitate a drastically curved parabolic surface as will be explained below.
Dielectric thin film coatings are commonly used to achieve high reflectivity in the NIR. However, these coatings are difficult to fabricate on surfaces of much curvature. All the commercial coating houses contacted during the project declined to become involved in a job of this nature.

Metal mirrors are the other possibility for reflective optics in the NIR. In particular, aluminum mirrors are both light weight and have a reflectance of over 96% at a wavelength of 1.65 μm at normal incidence\textsuperscript{221}. At other than normal incidence the reflectance increases and at any angle the reflectance is much greater than the total transmission for a multi-element refractive collimator. On this basis, an aluminum off-axis paraboloid of revolution was chosen as best for this project. Furthermore, for ease in aligning the mirror to the rest of the external cavity components, it was decided to use a right-angle off-axis paraboloid. That is to say, the axis of rotation of the paraboloid would be perpendicular to the axis of the diode laser emission.

The required dimensions, such as focal length and angular swing, for a right angle paraboloid may be determined with the help of Figure 6.1. The figure shows a cross-section parallel to the axis of revolution of the paraboloid. The restricting conditions on parameters displayed in the figure are as follows. The diode laser is located at (F,0,0) where F is the focal length of the paraboloid. $\alpha_1-\alpha_2$ must equal the beam divergence of the diode laser to gather most of the light emitted. $\frac{\alpha_1+\alpha_2}{2} = 90$ degrees so that the paraboloid is right angle off-axis. The positions along the y axis where the laser half-angle points intersect the parabola are $y_1$ and $y_2$. The apparent width of the diffraction grating as seen from the parabola is given by $y_2-y_1$. That is $y_2-y_1 = D\cos\theta$ where D is the width of the grating and $\theta$ is the
Figure 6.1 Cross-section of the external grating cavity parallel to optic axis of parabolic mirror.
angle of incidence of light on the grating which is \( \approx 30 \) degrees for a 600 l/mm grating. The width of the grating used for the present work is approximately 58 mm. Simultaneous solution of the expressions for \( \alpha_1 \) and \( \alpha_2 \) gives \( \alpha_1 = 125 \) degrees and \( \alpha_2 = 55 \) degrees. Substitution of the polar formula for a parabola into the above equations and solution for \( f \), the focal length of the parabola, yields \( f = 17.8519 \) mm.

Before proceeding with construction of an off-axis parabolic mirror the optical aberrations that would be present in the folded external cavity as shown in Figure 6.1 were determined.

6.4 Aberrations in an Off-Axis Parabolic Cavity

It was stated above that optical aberrations of an external cavity diode laser to grating coupler would be minimized with a parabolic collimator. It is the purpose of this section to show that such a mirror is indeed aberration free for the purposes at hand.

The cavity as shown in Figure 6.1 is optically equivalent to a folded Ebert-Fastie\textsuperscript{222} monochromator modified to use off-axis parabolic mirrors in a Littrow configuration\textsuperscript{223} as originally suggested by Welford\textsuperscript{224} where the normal monochromator entrance and exit slit function is accomplished by the small dimension of the laser active region. Ebert-Fastie-Welford (EBW) monochromators are now widely used and their optical properties have been thoroughly studied\textsuperscript{225-227}. It has been shown \textsuperscript{223} that EBW devices are third order aberration free near the optic axis.

To determine how critical the placement of the diode laser in the right angle cavity of Figure 6.1 would be in determining its optical aberrations, a computer ray tracing program was written to simulate the cavity. The program name is
CAVITY and Appendix F contains the basic language source listing of this program as written for the OGC Prime computer. The program carries out its calculations using geometrical optics ray tracing; no diffraction effects are introduced into the calculations. Additionally, no aberration effects are introduced for the diffraction grating since gratings in a Littrow configuration are anamorphic\textsuperscript{223,228}.

The program can perform three functions. First, it can display, with graphical assistance from the OGC Prime Graphics Editor, the simulated off-axis parabolic cavity with optical rays shown. There may be as many rays as are convenient for the program user. Furthermore, the rays may be initialized by either direct specification of their origin and initial direction or a two dimensional Gaussian angular probability distribution with two independent full-width half maximum angles may be specified for a given origin. Figure 6.2 shows a typical ray-trace output. In the figure, the rays leave from the focal point of the paraboloid with angles perpendicular to the active region of $\pm35, \pm25, \pm15,$ and $0$ degrees and at $0$ degrees in the plane of the junction.

Second, the program can calculate and display spot diagrams of the light returned to the diode laser facet. For this latter type of display it is advantageous to be able to determine the spot diagram for laser facets that have been rotated in the plane of Figure 6.2 or translated. This capability is integral to the program. Here, the Gaussian angular probability distribution provisions of the program may be used to simulate the beam divergence of the diode lasers as described in Chapter 4. Moreover, the program creates, when used in this mode, statistical data in separate Prime disk files on the the beam size perpendicular and parallel to the active region.
Figure 6.2 Graphic output from ray trace program CAVITY for the off-axis parabolic external grating diode laser cavity.
Figure 6.3 CAVITY generated spot diagram in the plane of the diode laser facet for Gaussian angular probability optical output distributions perpendicular and parallel to the active region. The diode laser is 30 µm from the optic axis of the parabola. The axes units are µm.
Figure 6.4  CAVITY generated spot diagram in the plane of the diode laser facet for Gaussian angular probability optical output distributions perpendicular and parallel to the active region. The diode laser is 15 \( \mu \text{m} \) from the optic axis of the parabola. The axes units are \( \mu \text{m} \).
Figure 6.5 CAVITY generated spot diagram in the plane of the diode laser facet for Gaussian angular probability optical output distributions perpendicular and parallel to the active region. The diode laser is 5 μm from the optic axis of the parabola. The axes units are μm.
Figures 6.3 through 6.5 show spot diagrams as generated by CAVITY. The figures represent the returning light spot for 100 rays initially launched from \((F,0,0)\) with Gaussian angular probability distributions both perpendicular and parallel to the active layer. Full width half maximum angles of 70 and 50 degrees, respectively, were used to generate the diagrams. In Figure 6.3, the laser facet has been translated 30 \(\mu m\) orthogonal to the axis of the paraboloid and away from it, i.e. away from the focal point. In Figures 6.4 and 6.5 the translation direction is the same but the distances are 15 and 5 \(\mu m\), respectively. From these figures it is easily seen that the spot size generated by the returning rays rapidly changes and so alignment along this direction is critical for optimal coupling of the returned light to the diode active layer. The spot diagram with no displacement shows a point spot on the scale of the previous diagrams. The radius of the spot is on the order of \(10^{-9}\) microns and the calculation is at this level double precision computationally limited. The operation for a properly placed diode is then aberration free and the figures indicate that placement of the diode laser along this direction must be within \(\pm 1\mu m\) for the aberration induced spot size to be less than the active region thickness. Similar diagrams with the ray origin at \((F, \pm 0.050mm, \pm 0.050mm)\) yield spot radii less than the active region thickness. The external grating cavity diode laser is therefore optically aberration free under the restricted use described here.

Last, the program when operated in the Gaussian angle mode creates a spot diagram in the plane of the grating. Figure 6.6 is a graphical representation of that diagram. It may be seen from the figure that the illumination at the grating is not uniform and thus diffraction effects are not simply dependent on the grating width.
Figure 6.6  CAVITY generated spot diagram in a plane orthogonal to the optic axis of the parabolic mirror and at the position of the grating. The axes units are mm.
7. AN EXTERNAL CAVITY SOURCE

The previous chapters have presented the requirements for and the optical design of an external grating cavity diode laser source for a DIAL methanometer. This chapter describes the construction and performance of such a source. Section 7.1 delineates the source mechanical construction. Section 7.2 explains the antireflection coating process used to minimize the coupling between the diode laser and its normal oscillation modes. In the third section, 7.3, an electronic wavelength control system is described. Also in that section, a dual diode pulser is described. The last section, 7.4, shows the source performance.

7.1 Mechanical Construction

Figure 7.1 shows the physical realization of the off-axis parabolic cavity described in Chapter 6 and schematically shown in Figure 6.2. The cavity includes a diamond-machined off-axis parabolic mirror, a diffraction grating mounted on a gimbal mount, a motorized micrometer for positioning the grating, a mount for two diode lasers, and a XYZ translation stage for positioning of the two diode lasers in the cavity. Each of the cavity components is described below.

Figure 7.2 gives a view of the off-axis parabolic mirror. The drastic curvature of the diamond machined surface is evident from the figure. Figure 7.3 is a repro-
Figure 7.1 The dual diode laser external off-axis parabolic mirror grating cavity source. Shown are the off-axis parabolic mirror, the grating and its positioner, and the dual diode laser mount and its positioner.
Figure 7.2  The off-axis parabolic mirror with the diamond-machined surface presented.
1. Material: Aluminum
2. All external dimensions in mm ± 1 mm except parabolic surface dimensions.
3. Focal length: 17.852 mm.
4. Threaded holes: 1/4"X28X3/8".
5. Surface figure: wavelength/2 over paraboloid @ 632.8 nm, minimum.
6. Surface roughness: less than 150 Angstroms (rms).
7. Surface A parallel to axis of paraboloid to within 20 microradians.

Figure 7.3  Technical specification drawing for mirror of Figure 7.2.
duction of the technical specification drawing for the mirror as given to Pneumo Precision, Inc. for machining in March 1983. The drawing was computer generated using the OGC Prime Graphics Editor. Included with the drawing are several technical requirements. In particular, the mirror is fabricated in aluminum with a 17.852 mm focal length as was suggested in Chapter 6. The surface figure is specified as λ/2 at a He-Ne laser wavelength which is equivalent to λ/5.2 at a wavelength of 1.65 μm. Also, the RMS surface roughness is required to be 150 Angstroms or less.

The finished mirrors were tested against the specifications in tests at Pneumo Precision and at OGC. The focal length and surface figure were examined for compliance with specifications at Pneumo Precision. The surface figure was shown to meet specifications using optical interferometric techniques. Acceptance tests conducted at OGC included measurements of the mirror reflectivity and total integrated scattering. Reflectivity at 45° incidence with 633 nm He-Ne laser light was measured to be 87% for the sum of the specularly reflected spot and the scattered light. Figure 7.4 shows a trace of light output versus angular position for one location on the mirror. In the figure, the small fluctuations to the sides of the center spot are scattered light and represent less than 5% of the total reflected light at 633 nm. The total integrated scattering (TIS) is inversely proportional to the square of the wavelength through the relation\(^{229}\)

\[
TIS = \left( \frac{4\pi \delta \cos(\theta)}{\lambda} \right)^2
\]  

(7.1)

where \(\delta\) is the RMS surface roughness, \(\lambda\) is the wavelength, and \(\theta\) is the angle of incidence. Using Equation 7.1 and the measurement at 633 nm the TIS at 1.65 μm
Figure 7.4  Surface reflected light vs. scattered angle for the mirror of Figure 7.2.
is calculated to be less than 1%. Coupled with the 87% reflectivity mentioned above and the higher reflectivity of aluminum at 1.65 μm, a specular reflectivity of 96% is calculated. The RMS surface roughness, calculated from the measured values for TIS, angle of incidence, and wavelength, is 160 Angstroms, which is within the measurement uncertainty of the 150 Angstrom specification.

The diffraction grating is a 600 l/mm replica fabricated with aluminum on epoxy on glass. It is blazed at 29° 41' for use in the first order at 1.6 μm in a Littrow configuration. Nominal reflectivity at 1.65 μm into the first order is 70%. The grating holder is an Ardel Gimbal 20-25 series mount.

There are three means by which the grating and gimbal mount could be automatically rotated and electronically controlled to ensure proper wavelength selection. The first method involves using piezoelectric translators attached to manual micrometers. This technique suffers from the high voltages (~ 1 kV) necessary to drive piezoelectric stacks over distances on the order of 1 μm. The second method involves use of micro-stepped stepper motors. The stepper motor technique is similar to that using DC motors with optical shaft encoder readout however the stepper motors are typically more bulky. The third method, and the one used for this project, entails use of DC motor driven micrometers with optical shaft encoder position readout.

The motorized micrometer shown in Figure 7.1 is an engineering run Ardel Kinamatic MotorMike™ Model 17213 with position readout capability. Position readout is achieved via TTL level electrical pulses from an optical shaft encoder and has a linear travel precision of 0.1 μm with a backlash limited accuracy of approximately 3 μm. A 0.1 μm position precision is equivalent, through the 1 inch lever angle of the gimbal mount, to a 4 microradian angular position precision.
Such precision is six times the angular resolution required as determined by Equation 6.4. The means by which this precision is converted to angular positioning accuracy is described in Section 7.3.

Double pulse LIDAR measurements, with an interpulse temporal separation of less than 1 ms, were shown in Section 5.4 to be advantageous from a signal processing standpoint. In Section 6.2, the concept of using two diode lasers in the same external grating cavity was introduced as a means of achieving a short interpulse period where the two lasers were placed at slightly different angles to the diffraction grating thus producing slightly different lasing wavelengths. The external cavity displayed in Figure 7.1 contains two such diode lasers in a brass mount.

Figures 7.5 and 7.6 are perspective drawings of the dual diode mount. Figure 7.7 is a close-up photograph of part of the same mount. In the figures, two lasers are shown to be positioned with their p contacts adjacent and contacting a gold strap conductor. The strap has approximate dimensions of 25 μm by 250 μm by 1 cm and was machined at OGC from 25 μm thick commercial Au foil with a frequency doubled Nd:YAG laser. The n contacts of the lasers rest on gold plated diamond heat sinks. Diamond heat sinks were chosen for this application because of their flat surface (cleaved planes) and parallel faces ( < 10') and because the thermal conductivity of Type IIa diamond is five times that of copper at room temperature. The lasers were hand positioned in the mount using a special function jig which featured an integral optical flat to ensure optical alignment of the diodes.

The aberrations in an off-axis parabolic grating cavity were discussed in Section 6.4. It was shown in that section that placement of the diode laser, regarding optical aberrations, was critical only along the optic axis of laser. The
Figure 7.5 Perspective drawing of the dual diode laser mount.
Figure 7.6  Detail drawing of the dual diode laser mount. Shown are the diode lasers and their heat sinks and indium bonding pads.
Figure 7.7  Photograph of that portion of the dual diode mount shown in Figure 7.6.
positioning stage shown in Figure 7.1 is a Klinger, Model MR-50, micropositioning device featuring manual micrometer adjustment in a plane parallel to the axis of rotation of the paraboloid and manual differential micrometer adjustment orthogonal to the axis. The former adjustments have a sensitivity of 1 \( \mu m \) while the latter has a sensitivity of 0.1 \( \mu m \). This precision is necessitated by the aberration requirements discussed in Section 6.4 and is achieved with an enhanced version of the standard MR-50. Before the diode lasers were mounted in the dual diode mount and installed in the external cavity, they were AR coated to decouple their light output from their normal cavity modes. The antireflection coating process is the subject of the next section.

### 7.2 Antireflection Coating

Dielectric thin films are often used for antireflection coatings on semiconductor devices. A dielectric film with index of refraction given by

\[
 n_f = \left( n_L n_{ext} \right)^{1/2}
\]

(7.2)

and thickness given by

\[
t = \frac{\lambda}{4n_f}
\]

(7.3)

gives a theoretical air-laser reflectivity of near zero (see Section 6.2). There are many methods\(^{238,239}\), including thermal evaporation, sputtering, plasma deposition, and chemical vapor deposition, by which such a coating might be applied to a diode laser. However, most AR coatings for light emitting diodes and diode lasers that have been reported in the literature\(^{240-243,183,185,179,203}\) have used coatings thermally or e-beam evaporated from SiO, although e-beam evaporation of ZrO\(_2\)\(^{185}\)
and sputtering of Si₃N₄ among other techniques have also been successful. Because of the large amount of information available about thermally evaporated SiO and its properties, this method of creating AR coatings was used on the present project.

The physical properties of evaporated SiO coatings have been well studied. The index of refraction of SiO rapidly evaporated (> 10 Angstroms/second) under vacuum conditions of less than 1 x 10⁻⁵ torr has been shown to be approximately 1.85 with negligible absorption near a wavelength of 1.65 μm. The effective index of refraction for the diode lasers used in the present project has been previously shown to be 3.52. Since the square root of 3.52 is 1.88, SiO can be seen, through Equation 7.2, to be a good AR material for these lasers.

There are two methods to achieve an optimum index-thickness combination for a single layer film. One method is to calculate the optimum index and thickness from the properties of the particular diode laser using guided wave theory and then to create those properties for the coating. This method requires strict knowledge and control of the coating process and has recently been put into use to sputter Si₃N₄ onto laser facets. The second, and much simpler, method uses a substance with approximately the right index of refraction as given by Equation 7.2 and then monitors the reflectivity looking for a minimum as the coating thickness increases. This technique was used on this project.

The SiO AR coatings were deposited from a Drumheller oven, Electronic Space Products, Inc. (ESPI) Part No. ESPI K4698C, using evaporation grade SiO, ESPI K4698C, at a background pressure of 10⁻⁷ to 10⁻⁶ torr. Figure 7.8 shows the setup for monitoring the reflectivity in real time. In the figure, the current pulser drives
Figure 7.8 Setup for in situ monitoring of the antireflection coating thickness during deposition.
the diode laser at a point below lasing threshold so that the diode emits only spontaneous emission. The light pipe shown in the figure carries light from the vacuum chamber to a Ge detector and preamp outside the chamber. The resultant signal was synchronously detected with a lockin amplifier, EG&G 5101, at the pulse repetition rate. The output from the lockin amplifier was recorded with a stripchart recorder. As the SiO coating was deposited the amount of light escaping the diode laser facet varied thus giving a record in real time of the coating efficiency.

Figure 7.9 shows the recorder output for a test AR coating deposited on a Laser Diodes Labs Model LCW-5 continuous wave 5 milliwatt optical output diode laser. The recorder plot is light output versus time. For this run a sine-wave generator was substituted for the pulser since the lockin amplifier intrinsically responds more efficiently to such a modulation signal. In the figure, each peak in light output indicates an odd multiple of quarter wavelengths for the coating thickness, while the troughs indicate a half wavelength thickness. The coating rate is approximately 16 Angstroms/second. The overall trend downward with time is caused by increased scattering and absorption in the coating. The after-coating reflectivity may be estimated from

\[ I_A = I_o \left(1 - R_A \right) \]  

(7.4)

and

\[ I_B = I_o \left(1 - R_B \right) \]  

(7.5)

where \( I_A \) and \( I_B \) are the laser light outputs after and before coating, respectively, \( I_o \) is the light intensity inside the facet, and \( R_A \) and \( R_B \) are the facet reflectivities after and before coating. Equation 7.5 may be divided into Equation 7.4 to solve for \( R_A \).
Figure 7.9 Optical output vs. time during deposition of a SiO antireflection coating on a Laser Diode Labs Model LCW-5 diode laser. The evaporation process is stopped at a 3 \( \lambda \) coating thickness.
using $R_B \approx 0.32$ for the LDL laser and the $\lambda/4$ peak in the figure. The resultant value of $R_A$ is 0.10 and would have been lower had not the device already had a commercial $\lambda/2$ coating on its output facet.

Figure 7.10 shows an example of a chart recorder trace for an AR coating applied to one of the diode lasers used in the present project. In this case, the evaporation process was terminated at a coating thickness of $\lambda/4$ to achieve minimum absorption and scattering. Calculation of the residual reflectivity in the manner presented above yields $R_A \approx 1\%$. After the coating was applied to the laser, which had a lasing threshold of 2 Amps before coating, it did not lase at currents greater than 6 Amps. Figure 7.11 shows a typical before- and after-coating light output versus drive current curve. In the figure, the lower curve is the light output from the uncoated facet after AR coating. The effect of the AR film on the lasing threshold is obvious from the figure.

The first attempts at AR film deposition were not as successful as those represented in the figures above: the early films tended to peel from the diode laser facet along lines parallel to the active region. The probable cause of this defect was determined to be anisotropic stress\textsuperscript{252} in the SiO film. Rotation of the evaporation angle of incidence to the laser facet from normal to 40 degrees off-normal eliminated the peeling problem. Subsequent film depositions exhibited another defect in which the films peeled off in narrow bands on the output facet along the facet intersection with the epitaxial layer interfaces. This type of defect occurred during prolonged operation in the external cavity and was attributed to localized heating at the interfaces, possibly due to nonradiative carrier recombination at those sites. Careful chemical pre-cleaning of the diode laser facets along with argon glow discharge sputtering of the facet just before evaporation eliminated this coating
Figure 7.10 Optical output vs. time during deposition of a SiO antireflection coating on an InGaAs/InP diode laser. The evaporation process is stopped at a $\lambda/4$ coating thickness.
Figure 7.11 Optical output vs. drive current for an InGaAs/InP diode laser before and after coating with SiO.
defect.

The cleaning and sputtering process was conducted as follows. After mounting of the diode lasers in their dual diode mount, the mount was ultrasonically washed in electronic grade acetone. After the washing was completed the mount was dried in a nitrogen jet. The mount was then placed in the evaporator and exposed for several minutes to Hg discharge-generated ozone to break down any residual hydrocarbons from the acetone wash. Then the vacuum chamber was evacuated to a background pressure of 500 mtorr of argon and glow discharge sputtering of the facet was achieved by placing the diode laser mount near the aluminum anode of a 2 mAmp/cm² current density discharge for several minutes. The discharge and subsequent film deposition were conducted in the presence of 200 mW of argon ion 514.5 nm laser light focussed on the facet. The laser light helped to keep the facet clean by heating it and by providing photons to the surface with energy greater than the binding energy of water vapor and hydrogen, the most common contaminants in high vacuum environments.

7.3 Electronic Construction

This section describes the electronic attributes of the dual diode laser cavity's wavelength controller and its current pulser. The wavelength controller was designed by this author and Mr. Robert Cary of Sunset Laboratory and OGC. The microprocessor coding was done by Mr. Cary. The electronic pulser was designed by Mr. John Hunt and constructed in the OGC electronics shop. Mr. Hunt is a Senior Electronics Engineer in the Applied Physics and Electrical Engineering Department at OGC. First, the wavelength controller will be described by paraphrasing and
summarizing its manual, "Dual Diode Cavity Wavelength Controller: Instrumentation for Automatic Laser Tuning". A definitive description of the controller, including hardware schematic diagrams and software code may be found in the manual. Second, the remaining part of the section will discuss the dual diode laser pulser.

The purpose of the wavelength controller is to cause automatic positioning of the grating angle relative to the external cavity so that maximum absorption in methane is achieved. The control process is designed to be a turn-key operation that is enabled whenever the diode laser electronics are turned on. Figure 7.12 is a block diagram of the physical layout of controller and its associated hardware. The hardware used in the controller consists of two circuits: the MotorMike (MM) motor control box and the analog signal board. Both of these connect to an Intel SBC 80/20 single-board computer.

The motor control box allows both forward and backward movement of the MM which positions the diffraction grating. It uses two of the TTL-compatible outputs from one 8255 Programmable Peripheral Interface (PPI) which is on board the 80/20. One output bit determines the motor direction while another bit turns the motor on and off.

The second circuit consists of analog signal conditioning amplifiers along with sample-and-hold (S/H) and analog-to-digital conversion (ADC) chips. This circuitry is constructed on a separate module which plugs onto one of the PPI edge connector ports. Two identical circuits are located on the module. The first circuit is for the reference optical signal and the second is dedicated to the signal from the optical power that has passed through a methane cell.

The signals are then conditioned. First, the reference and methane cell ger-
Figure 7.12  The wavelength controller and its associated hardware.
manium photodiode (Judson Infrared Model J-16) output is amplified using commercial preamps (Judson Infrared Model 700). The output from the preamps is then conditioned by a two-stage amplifier. The first stage is AC-coupled and noninverting with a gain of 12. This gain, coupled with that of the preamplifier, allows only a small portion of the optical output power to be used for this measurement. The next stage has a gain of 3 and includes an offset adjustable input. The offset allows the operator to calibrate a zero signal value while the light to the photodetectors is blocked.

The conditioned signals then go to sample-and-hold chips. These chips, as well as the following analog-to-digital converters, are controlled by the outputs from a dual monostable pulse generator which in turn is controlled by the TTL output of signal B from the diode laser pulser. The monostable pulse generator pulse widths are independently adjustable. This allows the operator to set the S/H-ADC operation to occur at the maximum for each photodetector pulse thus compensating for any difference in the time constants of the two channels. The rising edge of the pulse causes the S/H amplifiers to start sampling and sets up the ADCs. The falling edge of the pulse then causes the S/Hs to hold the peak value and simultaneously starts the conversions by the ADCs. The signal pulse from the optical detectors and their preamps and amplifiers occurs about 2 microseconds after the laser fires. After the ADC, the computer, which has been interrupted by the same TTL output B from the laser pulser, acquires the digital data.

The controlling software is written in assembly code and is stored in EPROMs. A complete listing of the software code is available in the controller manual. The code is located by functional blocks on separate EPROMs as follows. The first block contains power-up and interface chip initializations. The second block includes
several mathematical and setup routines called by the main operating system. The third EPROM includes several routines. One routine does 64 ADCs for each laser and then returns the ratio of the sums. Another scans the MM over a predetermined wavelength range seeking the minimum transmission through the methane cell. Other routines on this EPROM back up the MM to a predetermined point for rescanning of wavelength and output to a monitor raw signal values from each laser.

The main operating program contains the following functions:

1. Back up the MM 1024 counts (5.7 nm or 21 cm⁻¹).
2. Scan forward 2048 counts (11.5 nm) moving the MM 3 or 4 counts (~0.02 nm) each time saving the position where the minimum transmittance through the methane reference cell occurs.
3. Back up 128 counts beyond where the minimum was found.
4. Scan forward 256 counts, moving about 2 counts each time and again determine the location of minimum transmittance.
5. Compute a threshold value above the minimum value which will be looked for on the final scan. This has been implemented as 1/16 of the difference between the maximum and minimum ratios found during the first two scans but may be arbitrarily set.
6. Back up 64 counts beyond the most recently found minimum.
7. Scan forward, moving 1 count each time, until the threshold value is found.

The schematic diagrams for the dual diode current pulser are shown in Figures 7.13 and 7.14. Figure 7.13 shows the pulser timing circuitry. Figure 7.14 displays one channel of the current driver.
Figure 7.13 Timing circuitry for the dual diode laser pulser.
Figure 7.14 One current driver channel of the dual diode laser pulser.
The timing circuitry shown in Figure 7.13 has several notable features. The pulse repetition frequency may be set with the pulse rate potentiometer for interpulse periods of 0.1 to 1 ms. Another potentiometer controls the pulse width with a range of 100 to 300 ns available. An external enable (ground to disable) connector is provided to remotely turn the pulser on or off. Other external connection signals include a square wave synchronization signal at the PRF rate and TTL level pulse outputs, A and B, coincident in time with the laser current pulses. These three synchronization pulses allow for timing of external devices. Use of Pulse B was described above.

The diode driver shown in Figure 7.14 also has several notable features. The laser diode may be driven with a 0 to 10 Amp current pulse by varying the laser diode power voltage from 0 to \( \approx 40 \) volts. This \( 4 \Omega \) effective dynamic resistance compares favorably with the commercial diode laser pulser, Laser Diode Labs (LDL) Model LPC-23C, used in the early parts of this study. The LDL pulser had an effective resistance of \( \approx 30 \Omega \) thus needing \( \approx 300 \) volts to drive the diode laser with 10 Amps. The improvement achieved is due to the use of low on-impedance FETs, IRF521, instead of SCRs as in the LDL devices. The rise time of the current pulse is approximately 15 ns when the diode laser is mounted at the pulser output and slightly longer when an external BNC cable connects to the laser. The driver has external connections that supply the current pulse waveforms using a single American Laser Systems Model 711 inductive current probe. Current to the dual diode laser mount is also supplied through external BNC connections.
7.4 Source Performance

This section presents the optical output characteristics of the dual diode laser source described in the last three sections. Specifically, the wavelength bandwidth and tunability are explained. The absorption of the optical output in methane is also discussed. Finally, automatic tuning of the diffraction grating to an absorption maximum in methane is demonstrated.

Figure 7.15 shows the tuning range accessible by the dual diode external cavity. The figure was generated by focusing the light output from one diode laser in the dual cavity onto the slit of a Jarell-Ash Mark-X 0.27 m spectrometer and scanning wavelength while synchronously detecting the spectrometer output with a Ge detector and lockin amplifier. It can be seen from the figure that a wavelength range of 1.624 to 1.648 (6158-6068 cm⁻¹) was achieved in this instance. In other cases, both slightly shorter and longer wavelengths have been achieved. It may be seen that the spectral range of the figure includes several lines, notably R₆, of the 2ν₃ overtone band which was described in Chapter 3. However, not all wavelengths in this range were attainable.

Higher resolution spectral scans over a smaller region were in some instances conducted by placing a Fabry-Perot interferometer between the spectrometer output and the Ge detector. The interferometer consists of a piezoelectrically scanned Fabry-Perot device (Burleigh Model RC-110) driven by a dedicated ramp generator (Burleigh Model RC-42). The lockin amplifier output was then plotted on a chart recorder while holding the dual cavity grating fixed or the detector output was viewed on an oscilloscope screen while scanning the cavity grating. Figure 7.16 is an example of the chart recorder output. For this figure, the Fabry-Perot mirror
Figure 7.15 An example of the tuning range accessible by the dual diode external cavity.
Figure 7.16 Optical output vs. Fabry-Perot mirror displacement for the dual diode external cavity.
separation was 0.013" yielding an interferometer free spectral range of 41 Angstroms. That is to say that the wavelength separation between the major peaks in the figure is 41 Angstroms. The slits of the spectrometer were adjusted to match this spectral range. From the figure, the calculated linewidth (FWHM) is 1.4 Angstroms.

When the output was viewed on an oscilloscope and the grating was rotated, it was seen that for some positions of the grating the residual diode laser cavity modes, as determined by blocking the grating feed back while observing the spectrum, would appear. This was the cause of the inability mentioned above to achieve all wavelengths encompassed by the range of Figure 7.15. The source of such residual laser cavity modes is residual reflectivity which indicates that a more efficient AR coating would be required for more continuous tuning. It was also observed that tuning tended to be less efficient with usage over several days indicating possible degradation of the coatings.

Measurements of the optical absorption in a 30 cm methane cell were conducted. The cavity was tuned so that maximum absorption was attained for one diode while at the same time negligible absorption occurred for the other diode. The methane in the cell was at atmospheric pressure. The maximum absorption observed in the cell was slightly over 65%, which is equivalent to an absorption coefficient of 0.04 cm⁻¹atm⁻¹. In contrast, the maximum achievable absorption as shown in Figure 3.9 for a laser bandwidth of 0.2 cm⁻¹ would be 0.15cm⁻¹atm⁻¹. The increased spectral bandwidth described above is the cause of the decreased absorption.

To demonstrate the activity of the wavelength controller, the amount of absorption in the cell was also measured and recorded on magnetic tape by the wavelength controller described in Section 7.3 as it rotated the grating over a range
near maximum absorption seeking the minimum cell transmission. Figure 7.17 shows data for one wavelength search as stored on the tape. Although maximum absorption was not seen during this experiment because of inadequate cavity optical alignment, it can be seen in the figure that the dual diode laser output scans through a minimum in transmission and then retraces its steps through the minimum again. What is not shown in the figure is the final scan described in Section 7.3.
Figure 7.17: An example of the absorption as a function of wavelength measured by the dual diode laser cavity wavelength controller.
8. CONCLUSIONS

This research project has encompassed two tasks. The first was a study conducted to determine if room-temperature injection lasers could be used as the source for a DIAL methanometer for coal mine applications. As part of that study, prior DIAL measurements of methane were reviewed and the measurement technique was explored in a general way as reported in Chapter 2. Then, the absorption spectroscopy of methane was examined in detail and found to contain an appropriate absorption feature near a wavelength of 1.65 μm when the spectral width of the light source was approximately 0.2 cm\(^{-1}\). The spectroscopic studies are explained in Chapter 3. As an additional part of the study the operating characteristics of broad area high optical output InGaAs/InP injection lasers were examined. Chapter 4 reports on the operating characteristics found. A detailed calculation of the requirements for a diode laser DIAL measurement of methane in a coal mine was then carried out as presented in Chapter 5. By comparison of the diode laser properties reported in Chapter 4 with the DIAL requirements developed in Chapter 5, it was found that broad area InGaAs/InP injection lasers were suitable in most respects for coal methane measurements. The exception was the diode laser spectral bandwidth. It was found to be some 400 times too large.

The second task was the design and fabrication of an external grating cavity to reduce the bandwidth of the injection lasers described in Chapter 4. Chapter 6
develops the optical design of an off-axis parabolic mirror grating cavity. Using geometric optical design, the desired spectral bandwidth of 0.2 cm⁻¹, was used to determine the physical parameters for the external cavity. Chapter 7 describes the fabrication and performance of the external resonator source. The source was found to have a narrowed bandwidth two to three times larger than designed. An explanation of the resultant bandwidth based on coupled mode theory is presented in Chapter 7 and Appendix E. In summary, an external grating cavity for a diode laser was assembled which was able to approximate the optical properties required for a DIAL coal mine methane measurement.

Coupled cavity diode lasers may provide a convenient means to achieve the narrow spectral bandwidth and the high optical output necessary for remote sensing applications in coal mines. Cleaved-coupled-cavities (C³) have previously been used²⁵⁵-²⁵⁹ to obtain frequency-stable, tunable, single-longitudinal mode operation in index-guided, single-emitter, InGaAsP diode lasers with optical outputs ranging from 0.5 to 2.5 mW. Recently, DeFreez et al. reported²⁶⁰ CW operation of a C³ phase-locked array of gain-guided GaAlAs lasers. They obtained tunable, single-longitudinal mode operation to output powers as high as 50 mW as well as control of the radiation pattern emitted by the array. It is the opinion of the author that there are no fundamental physical obstacles to transferring this technology to the longer wavelength InGaAsP diode laser family. Thus, it would seem that small, efficient, safe sources for remote measurements of methane for coal mine, as well as other, applications can be available in the very near future.
References

17. W. T. Tsang, “Al_{0.48}In_{0.52}As/Ga_{0.47}In_{0.53}As/Al_{0.48}In_{0.52}As double-heterostructure lasers grown by molecular-beam epitaxy with lasing wavelength at 1.65 μm,” *J. Appl. Phys.*, vol. 52, pp. 3861-3865, Jun. 1981.


20. W. D. Egan. Homer Research Laboratories, Bethlehem Steel Corporation, Private Communications


73. K. Fox, G. W. Halsey, and D. E. Jennings, "High resolution spectrum and analysis of \(2\nu_3\) of \(^{13}\text{CH}_4\) at 1.67 \(\mu\)m," J. Mol. Spectrosc., vol. 83, pp. 213-222, 1980.


89. B. Bobin, "Interpretation de la bande harmonique 2v$_3$ du methane $^{12}$CH$_4$ (De 5,890 A 6,107 cm$^{-1}$)," *J. Physique*, vol. 33, pp. 347-352, Apr. 1972.


100. K. J. Bachmann and J. L. Shay, "An InGaAs detector for the 1.0-1.7-$\mu$m wavelength range," *Appl. Phys. Lett.*, vol. 32, pp. 446-448, 1 Apr. 1978.


APPENDIX A

This appendix lists the computer source program used to generate data for plots of optical transmission versus wavenumber, for a specified methane concentration, and for a specified spectral resolution. Plots for the P, Q, and R branches of the $2\nu_3$ methane absorption so generated are shown in Figures 3 through 11 in Chapter 3.

This program is a modification of a listing presented in an AFCRL document\textsuperscript{261}.
LEVEL 2.3.0 (JUNE 18)

REQUESTED OPTIONS:

PROGRAM BY RICK OUAEEZ

THIS PROGRAM GENERATES A TRANSIENT SPECTRUM WITH INPUT

RESULTS DEPENDENT UPON THE ACTUAL PRESSURE BOUNDARY VALUES.

PROGRAMMED FOR A NUCLEAR REACTIONS.

CALCULATIONS ARE PERFORMED FOR A UNIFORM SLOWER PRESSURE.

SLOW TEMPERATURE PATH CONSIDERING THE ATOMIC SYSTEMS IN THE

INPUT SPECIFICATIONS. A MULTIPLE SPECIFICATIONS MUST

INCLUDED IN A SINGLE MOLECULAR SYSTEMS.

SLOW, MEDIUM-SLOW, FAST, AND HISHER.

SLOW FUNCTION OF SECOND HARMONIC AMPLITUDE DISSIPATING

CHROMATIC RESULTS.

THE PROGRAM USES A WAVELENGTH A TO CONVOLVE WITH THE WAVE-LENGTH.
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**Notes:**
- If \( |Z_2 - IT| > 5000 \) calculation cannot be done.
- If there are more than 5000 lines in the frequency range, calculation cannot be done.
- Rotational partition function is defined below.
- Temperature dependence of all lines intensities computed here.
- Define indices 15 and 16 indicating which spectral lines are to be used in the calculation of frequency.
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160 0010 GO 35 115.11
160 0011 IF (V-J)/DUP=-GND*F179.29.33
160 0012 GO 268
160 0013 GO TO 34
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APPENDIX B

This appendix presents a safety calculation for a 1.6 μm collimated repetitively pulsed diode laser. It is based on the "American National Standard for the Safe Use of Lasers"\textsuperscript{262}. The explanation below is paraphrased from Section B.3.1.2 of that document. The calculation presented is similar to Example 4 therein.

To determine the maximum safe exposure for a repetitively pulsed laser, the wavelength, PRF, duration of a single pulse, and duration of a complete exposure must be known. This determination requires two analyses and a conclusion. Steps 1 and 2 and Step 3, respectively, in the following calculation.

The calculation determines the intrabeam direct-viewing exposure for an In\textsubscript{0.53}Ga\textsubscript{0.47}As/InP (λ ≈ 1.6 μm) laser of pulse duration (\(\tau\)) equal to 100 ns and PRF = 10 kHz. Since the 1.6 μm wavelength light will not cause a natural eye aversion response, as a visible-wavelength laser would, a 1 second exposure duration (T) is assumed.

Step 1. Individual Pulse Limitation

This step requires the calculation of the maximum exposure based on the limitation that a single-pulse exposure shall not exceed the single pulse maximum per-
missible exposure (MPE) (ANSI Sections 8.5.1.1 and 8.5.1.5) multiplied by a correction factor (F_1) of ANSI Figure 12. From that figure, F = 0.06 for a PRF = 10 kHz. The maximum exposure for an individual pulse is given by

\[ H_i = F_1 \text{(MPE)} = (0.06)(10^{-2} \text{ Jcm}^{-2}) = 6.0 \times 10^{-4} \text{ Jcm}^{-2}. \]  

(B.1)

On this basis, the maximum exposure for a train of pulses is given by

\[ H = H_i \text{(PRF)}T = (6.0 \times 10^{-4})(10^3 \text{ Hz})(1 \text{ Sec}) = 6 \times 10^{-1} \text{ Jcm}^{-2}. \]  

(B.2)

**Step 2. Average Power Limitation**

The average power limitation requires the calculation of the total radiant exposure for the total pulse duration. From ANSI Figure 6, for T = 1 Sec the maximum exposure is given by

\[ H = 5.6 \times 10^{-1} \text{ Jcm}^{-2}. \]  

(B.3)

**Step 3. Conclusion**

Comparing the results of Step 1 and Step 2, the more restrictive limitation applies. Step 2 is more restrictive and hence applicable. This implies that the maximum single pulse exposure is given by

\[ H_i = 5.6 \times 10^{-5} \text{ Jcm}^{-2}. \]  

(B.4)

This result then gives a peak power density for each pulse

\[ D_p = \frac{H_i}{\tau} = \frac{5.6 \times 10^{-5} \text{ Jcm}^{-2}}{10^{-7} \text{ Sec}} = 550 \text{ Wcm}^{-2}. \]  

(B.5)
Assuming a 1 mm laser beam diameter (ANSI Section 3.2.3.3), the resulting peak power is

\[ P_p = D_p \pi \frac{D^2}{4} = 4.3 \, \text{W} \quad \text{(B.6)} \]

where \( D \) is the beam diameter. This power value is the upper limit to exempt laser status.
APPENDIX C

The relationship between the RDIAL measurement accuracy and the measurement precision of voltage is presented in this appendix. This relationship is derived from the fundamental RDIAL expression, Equation 2.5.

The derivation proceeds in two steps. In the first step, Equation 2.5 is inverted to solve for the gas concentration implicit in the absorption coefficient. In the second step, error propagation analysis is applied to the inverted Equation, C.17.

C.1 Inversion

The fundamental expression, Equation 2.5, is given by

\[ P_r(R) = \left( \frac{\beta \Delta R}{4\pi} \right) K P_o \left( \frac{A}{R^2} \right) e^{-2\int_0^R a(r)dr} \]  

(C.1)

where \( \beta \) = Mie backscatter coefficient, \( \Delta R \) = sample depth, \( R \) = distance to the sample volume center, \( P_o \) = power transmitted, \( P_r \) = power returned, \( K \) = optical system efficiency, \( A \) = receiver area, and \( a \) = methane absorption coefficient.

As is explained in Chapter 5, the geometrically range resolved DIAL process requires two light pulses each returning light from two locations, at \( R_1 \) and \( R_2 \), respectively. In what follows, pulse \#1 refers to the on absorption line pulse in the
DIAL process. Pulse #2 refers to the off line pulse. Also, \( R_2 - R_1 = \Delta R \). For pulse 

\#1:

\[
P_{r, on}(R_2) = \frac{\beta_{\text{Mis}}(R_2)}{4\pi} K_2 A_2 P_{o,1} \frac{\Delta R}{R_2^2} \exp \left\{ -2\bar{\alpha}_{\text{ABS, on},2} R_2 \right\} \tag{C.2}
\]

\[
P_{r, on}(R_1) = \frac{\beta_{\text{Mis}}(R_1)}{4\pi} K_1 A_1 P_{o,1} \frac{\Delta R}{R_1^2} \exp \left\{ -2\bar{\alpha}_{\text{ABS, on},1} R_1 \right\}. \tag{C.3}
\]

For pulse 

\#2:

\[
P_{r, off}(R_2) = \frac{\beta_{\text{Mis}}(R_2)}{4\pi} K_2 A_2 P_{o,2} \frac{\Delta R}{R_2^2} \exp \left\{ -2\bar{\alpha}_{\text{ABS, off},2} R_2 \right\} \tag{C.4}
\]

\[
P_{r, off}(R_1) = \frac{\beta_{\text{Mis}}(R_1)}{4\pi} K_1 A_1 P_{o,2} \frac{\Delta R}{R_1^2} \exp \left\{ -2\bar{\alpha}_{\text{ABS, off},1} R_1 \right\}. \tag{C.5}
\]

In Equations C.2 through C.5 the superscript bar indicates the average absorption coefficient over the given range \( R \). Also, \( \alpha = \alpha_{\text{ABS}} \) as explained in Chapter 5.

Writing the light powers of the above equations as voltages through the use of square law detectors, the following definitions are made:

\[
N_{\text{on}} = \ln \left[ \frac{V_{r, on}(R_2)}{V_{r, on}(R_1)} \right] \tag{C.6}
\]

and

\[
N_{\text{off}} = \ln \left[ \frac{V_{r, off}(R_2)}{V_{r, off}(R_1)} \right] \tag{C.7}
\]

As a first step toward inversion of Equations C.2 through C.5, substitution of
those equations into C.6 and C.7 and subtraction gives:

\[ N_{on} - N_{off} = -2\bar{\alpha}_{ABS,on,2}R_2 + 2\bar{\alpha}_{ABS,on,1}R_1 + 2\bar{\alpha}_{ABS,off,2}R_2 - 2\bar{\alpha}_{ABS,off,1}R_1. \]  \hspace{1cm} (C.8)

It is convenient to introduce the following definitions:

\[ \bar{\alpha}_{ABS,on,2} \equiv \bar{\alpha}_{ABS,on,1}R_1 + \bar{\alpha}_{ABS,on}(R_2 - R_1) \]  \hspace{1cm} (C.9)

and

\[ \bar{\alpha}_{ABS,off,2} \equiv \bar{\alpha}_{ABS,off,1}R_1 + \bar{\alpha}_{ABS,off}(R_2 - R_1). \]  \hspace{1cm} (C.10)

Here \( \bar{\alpha}_{ABS,on} \) is the average value of \( \alpha_{ABS,on} \) on \([R_1, R_2]\) and likewise for the off component.

The inversion is then nearly complete with the following observation:

\[ N_{on} - N_{off} = 2(R_1 - R_2)(\bar{\alpha}_{ABS,on} - \bar{\alpha}_{ABS,off}) \]  \hspace{1cm} (C.11)

The absorption coefficients may be written as a product of the average gas concentration and the absorption cross section as follows:

\[ \bar{\alpha}_{ABS,on} = C \sigma(\lambda_{on}) \]  \hspace{1cm} (C.12)

and

\[ \bar{\alpha}_{ABS,off} = C \sigma(\lambda_{off}) \]  \hspace{1cm} (C.13)

where \( \sigma \) is the absorption cross section at wavelength \( \lambda \) and \( C \) is the average gas concentration on \([R_1, R_2]\). The average gas concentration may then be written:
The inversion of Equation C.1 for the gas concentration is complete with the exception that the two $\sigma$ variables have yet to be expressed in terms of measurable parameters.

The variables $\sigma_{on}$ and $\sigma_{off}$ can be calculated from:

$$T = \exp \left[ -\sigma(\lambda_{on})C' \right] = \frac{V_{on,2}}{V_{on,1}}$$  (C.15)

$$T = \exp \left[ -\sigma(\lambda_{off})C' \right] = \frac{V_{off,2}}{V_{off,1}}$$  (C.16)

where $C'$ is the known gas concentration in a reference cell, $l = r_2 - r_1$, the length of the reference cell, and $V_{on}$ and $V_{off}$ are reference detector voltages. The completed inversion of Equation C.1 is given by:

$$C = \frac{C'(r_2 - r_1)}{2(R_1 - R_2)} \frac{\ln \left( \frac{V_{r,off}(R_2)}{V_{r,off}(R_1)} \right)}{\ln \left( \frac{V_{on,1}}{V_{on,2}} \right)} - \ln \left( \frac{V_{r,off}(R_2)}{V_{r,off}(R_1)} \right)$$  (C.17)

C.2 Error Propagation

Error propagation analysis is now applied to the inverted Equation C.17. The analysis is carried out in terms of standard deviations of the various measured voltages and the calculated methane concentration.
The standard deviation in the concentration for small, random, and uncorrelated voltage fluctuations is given by:

$$\sigma_c = \left[ \sum_{i=1}^{n} \left( \frac{\partial c}{\partial V_i} \frac{\sigma_{V_i}}{V_i} \right)^2 \right]^{1/2}$$

(C.18)

where $\sigma_x$ represents the standard deviation in $x$. The partial derivative factors in C.18 may be written:

$$\left[ \frac{\partial c}{\partial V_i} \right] = \left[ \kappa \frac{1}{V_i} \right]$$

(C.19)

where $\kappa$ is given by:

$$\kappa = \pm \frac{C'(r_2-r_1)}{2(R_1-R_2)} \ln \left( \frac{V_{on,1}}{V_{on,2}} \right) - \ln \left( \frac{V_{off,1}}{V_{off,2}} \right)$$

(C.20)

for the returned signal voltages, $V_r$, and

$$\left[ \frac{\partial c}{\partial V_i} \right] = \left[ \kappa' \frac{1}{V_i} \right]$$

(C.21)

where $\kappa'$ is given by:

$$\kappa' = \pm \frac{C'(r_2-r_1)}{2(R_1-R_2)} \ln \left( \frac{V_{r,off}(R_2)}{V_{r,off}(R_1)} \right) - \ln \left( \frac{V_{r,off}(R_2)}{V_{r,off}(R_1)} \right)^2$$

(C.22)

for the references voltages.
The assumption is made that equal signal to noise ratios can be achieved for each measured return voltage. That is, assume:

\[
\begin{bmatrix}
\sigma_y \\
V
\end{bmatrix}_i = \begin{bmatrix}
\sigma_y \\
V
\end{bmatrix}_j = \frac{\sigma_y}{V}
\]  

(C.23)

for all \(i\) and \(j\) for the returned signals. Also it is assumed that the reference signal to noise ratios are much greater than the returned signal ratios due to the larger optical power available to the reference detectors. If the reference cell gas concentration is adjusted to obtain the absorption typically found in the remote sample volume (i.e. population distribution of absorbing molecules and pressure broadened linewidths are the same)\(^{264}\), the following approximations can be made:

\[
\ln \left[ \frac{V_{r, off}(R_2)}{V_{r, off}(R_1)} \right] \approx \ln \left[ \frac{V_{on,2}}{V_{on,1}} \right] \quad \text{and} \quad \ln \left[ \frac{V_{r, off}(R_1)}{V_{r, off}(R_1)} \right] \approx \ln \left[ \frac{V_{off,1}}{V_{off,2}} \right]
\]  

(C.24)

Equation C.24 implies \(\kappa \approx \kappa'\).

Substitution of C.23 into C.18 then gives:

\[
\sigma_c = \frac{2\sigma_y |\kappa|}{V}
\]  

(C.25)

where the \(\kappa'\) term is removed because of the large reference signal to noise ratios.

Substitution of Equation C.20 into Equation C.25 divided by Equation C.17 yields:

\[
\frac{\sigma_c}{C} = \frac{2 \sigma_y}{V} \ln \left[ \frac{V_{r, off}(R_2)}{V_{r, off}(R_1)} \right] \ln \left[ \frac{V_{r, off}(R_2)}{V_{r, off}(R_1)} \right]
\]  

(C.26)

Since the absorption cross section is small in the off line portion of the RDIAL process, simplifications can be made to Equation C.26. Specifically, the small
amount of absorption implies:

\[
\frac{V_{r,\text{off}}(R_2)}{V_{r,\text{off}}(R_1)} \approx 1
\]  
(C.27)

Finally, substitution of Equation C.27 into Equation C.26 gives a simple expression for the maximum allowable normalized standard deviation in the measured voltages as a function of the required gas concentration measurement accuracy and the amount of absorption in the sample volume during the on line portion of the RDIAL process:

\[
\frac{\sigma_v}{V} = \frac{1}{2} \frac{\sigma_c}{C} \ln \left( \frac{V_{r,\text{on}}(R_2)}{V_{r,\text{on}}(R_1)} \right)
\]  
(C.28)
APPENDIX D

Standard expressions for, and numerical values of, the various detection noise sources of Section 5.3 are presented in this appendix.

D.1 Background Noise

Here it is assumed that the detection system views, in addition to signal back-scattered from coal dust, a Lambertian blackbody wall. The wall is assumed to be at temperature of 20°C. The optical power received by the detection system is given by

\[ P_{r, BB} = W_{\Delta \lambda} A \Omega_0 \Delta \varepsilon \]  

(D.1)

where \( W_{\Delta \lambda} \) is the spectral blackbody radiance, \( A \) is the area of the sources seen, \( \Omega_0 \) is the solid angle of the receiver optics subtended at the source, \( \Delta \lambda \) is the spectral bandwidth of the receiving system (\( \approx 10 \text{ nm} \)), and \( \varepsilon \) is the source emittance which is assumed to be \( \frac{1}{\pi} \). This implies

\[ P_{r, BB} = 1 \times 10^{-13} \text{ watts} \]  

(D.2)

where numerical values typical to the HRL methane detection system have been
used. The calculated optical power yields the following background averaged squared noise current:

\[
\overline{i_D^2} = \frac{3e^2 P_r BB \eta \Delta \nu}{h \nu} = 3 \times 10^{-22} \Delta \nu \text{ Amps}^2
\]  

\[(D.3)\]

where \(e\) is the electronic charge, \(\eta\) is the detector efficiency (≈0.5), \(\Delta \nu\) is the detection system electronic bandwidth in Hz, \(h \nu\) is the laser photon energy, and where 100% optical efficiency has been assumed. Additionally, an implicit assumption of no artificial light sources in the detector field of view was made.

### D.2 Detector Dark Current Noise

The averaged squared detector dark current for photodiodes, which are typically used in the near infrared, is given by

\[
\overline{i_D^2} = 2e i_d \Delta \nu = 3 \times 10^{-19} i_d \Delta \nu \text{ Amps}^2
\]  

\[(D.4)\]

where \(i_d\) is the detector dark current in Amps.

### D.3 Signal Shot Noise

The averaged squared signal shot current is given by

\[
\overline{i_{SN}^2} = \frac{3e^2 P_r \eta \Delta \nu}{h \nu} = 3 \times 10^{-28} \Delta \nu \text{ Amps}^2
\]  

\[(D.5)\]

where a returned optical power, \(P_r = 10^{-9}\) watts is assumed.
D.4 Load (Johnson) and Amplifier Noise

The averaged squared load and amplifier current noise for a voltage amplifying circuit is given by

\[ \overline{\eta_A^2} = \frac{4K_B T_e \Delta \nu}{R_L} \]  

(D.6)

where \( R_L \) is the load resistance, \( K_B \) is the Boltzmann constant, and the equivalent temperature is given by

\[ T_e \approx (F)(290^\circ K) \]  

(D.7)

where \( F \) is the noise figure of the amplifier. A typical value of good amplifiers is \( F = 1.3; T_e \approx 380^\circ K \). \( R_L \) is limited by the system time constant, \( \tau \), through the relation

\[ \tau = R_L C \]  

(D.8)

where \( C \) is the total amplifier input capacitance. This implies

\[ R_L = \frac{1}{2\Delta \nu C} \]  

(D.9)

Thus the averaged squared noise current is given by

\[ \overline{\eta_A^2} = 8K_B T_e C(\Delta \nu)^2 \]  

(D.10)

where \( C \) is in units of farads. Substitution of a typical capacitance value\(^{256},\)

\[ C = 10^{-11} \text{ F} \]

for a small area Ge photodiode at zero bias gives
\[ i_A^2 = 4 \times 10^{-31} (\Delta \nu)^2 \text{Amps}^2 \] (D.11)
APPENDIX E

This appendix presents a derivation of the spectral bandwidth for the off-axis parabolic mirror/grating diode laser cavity used in this project. This derivation uses, as was mentioned in Section 6.2., coupled mode theory as its basis.

Figure E.1 shows schematically an external grating diode laser cavity. The spatial dependence perpendicular to the diode active region of the laser waveguide circulating mode and the optical mode incident on the laser facet may be written, respectively, as:

\[ \Psi_L(z=0) = A \exp \left[ \frac{-x^2}{\omega_0^2} \right] \]  \hspace{1cm} (E.1)

and

\[ \Psi_i(z=0) = A' \exp \left[ \frac{-(x-a)^2}{(\beta \omega_i)^2} \right] \]  \hspace{1cm} (E.2)

where \( \omega_0 \) is the spotsize of the waveguide circulating mode in the diode laser, \( \beta \) is the ratio of the spotsize of the incident wave to that of the guided wave, \( a \) is the relative displacement in the x direction of the two spots, and \( A \) and \( A' \) are proportionality constants.

The coupling efficiency between the guided and incident modes is given by\textsuperscript{267,268}
Figure E.1  Schematic representation of the dual diode laser cavity showing the diode laser circulating guided wave and the grating returned optical mode.
This implies by substitution that \( \eta \) may be written as

\[
\eta(a, \beta) = \frac{\int_{-\infty}^{\infty} \exp \left[ -\frac{x^2}{\omega_0^2} - \frac{(x-a)^2}{(\beta \omega_0)^2} \right] \, dx}{\int_{-\infty}^{\infty} \exp \left[ -\frac{2x^2}{\omega_0^2} \right] \, dx \int_{-\infty}^{\infty} \exp \left[ -\frac{2(x-a)^2}{(\beta \omega_0)^2} \right] \, dx}
\]  

(E.4)

Evaluation of the integrals in Equation E.4 leads to the following expression for \( \eta \)

\[
\eta(a, \beta) = \frac{2\beta}{\beta^2+1} \exp \left[ \frac{-2a^2}{\omega_0^2 \left( \beta^2+1 \right)} \right]
\]  

(E.5)

In Figure E.1, \( 2a = f \Delta \theta \) where \( f \) is the focal length of the focusing optics and where \( \Delta \theta \) is the full width angular deviation of the grating feedback light from the center wavelength. Substitution of Equation E.5 into the fundamental dispersion relation for a Littrow mounted grating\(^{269}\)

\[
\Delta \theta = \frac{2 \tan(\theta) \Delta \lambda}{\lambda}
\]  

(E.6)

yields

\[
\eta = \frac{2\beta}{\beta^2+1} \exp \left[ \frac{-2(f \tan(\theta) \Delta \lambda)^2}{\lambda^2 \omega_0^2 \left( \beta^2+1 \right)} \right]
\]  

(E.7)

It is known that\(^{270}\)

\[
I_{th} \propto a + \frac{1}{2L} \ln \left( \frac{1}{R_1 R_G} \right)
\]  

(E.8)
where $I_{th}$ is the laser threshold current, $\alpha$ represents the laser internal losses including the loss associated with the current required to achieve zero gain, and $L$ is the laser length, $R_1$ is the laser output facet power reflectivity and $R_G$ is the effective grating reflectivity.

$R_G$ may be expressed as:

$$R_G = R_m^2 \epsilon \eta$$  \hspace{1cm} (E.9)

where $R_m$ is the mirror reflectivity $\approx 0.95$, and $\epsilon$ is the Littrow mount grating efficiency $\approx 0.70$. Both $R_m$ and $\epsilon$ are nearly independent of wavelength on the scale of the present discussion. Let the following definitions be made:

$$I_o \equiv I_{th}(\lambda=\lambda_o)$$  \hspace{1cm} (E.10)

$$I_{\Delta\lambda} \equiv I_{th}\left\{\lambda=\lambda_o \pm \frac{\Delta\lambda}{2}\right\}$$  \hspace{1cm} (E.11)

$$Z_{\Delta\lambda} \equiv \frac{I_o}{I_{\Delta\lambda}}$$  \hspace{1cm} (E.12)

which implies that

$$Z_{\Delta\lambda} = \frac{\alpha + \frac{1}{2L} \ln \left\{ \frac{1}{R_1 R_m^2 \epsilon \eta_o} \right\}}{\alpha + \frac{1}{2L} \ln \left\{ \frac{1}{R_1 R_m^2 \epsilon \eta_{\Delta\lambda}} \right\}}$$  \hspace{1cm} (E.13)

where $\eta_o$ is $\eta(\lambda_o)$ and $\eta_{\Delta\lambda}$ is $\eta(\lambda=\lambda_o \pm \frac{\Delta\lambda}{2})$.

Let $R'$ be the current overdrive:

$$R' = \frac{1}{I_o}$$  \hspace{1cm} (E.14)
where $I$ is the diode laser drive current. Then if $R' > \frac{1}{Z_{\Delta\lambda}}$ the laser oscillator modes at $\lambda = \lambda_o \pm \frac{\Delta \lambda}{2}$ will be above lasing threshold and, conversely, if $R' < \frac{1}{Z_{\Delta\lambda}}$ those modes will be below threshold.

The optical power emitted into a mode near $\lambda = \lambda_o \pm \frac{\Delta \lambda}{2}$ is then given by

$$P_{\Delta\lambda} = \eta_D \left[ \frac{1}{I_{th}} - \frac{1}{Z_{\Delta\lambda}} \right] I_{th} \quad (E.15)$$

where $\eta_D$ is the laser external differential quantum efficiency and where the term in brackets must be non-negative to be meaningful. In the case that $Z_{\Delta\lambda} = 1$ (i.e. $R_{\Delta\lambda} = R_o$ or $\Delta \lambda = 0$) it may be seen that Equation E.15 reduces to the standard formula for output versus drive current:

$$P = \eta_D (I - I_{th}) \quad (E.16)$$

Substitution yields:

$$P_{\Delta\lambda} = \eta_D (R' - \frac{1}{Z_{\Delta\lambda}}) I_{th} \quad (E.17)$$

To find the spectral width (FWHM), $\Delta \lambda_{\frac{1}{2}}$, of the optical power, let

$$P(Z_{\Delta\lambda_{\frac{1}{2}}}) = \frac{1}{2} P(Z_{\Delta\lambda} = 1) \quad (E.18)$$

Define

$$Z_{\Delta\lambda_{\frac{1}{2}}} = Z' \quad (E.19)$$

Substitution of Equation E.19 into Equation E.18 and evaluation gives:

$$Z' = \frac{2}{R' + 1} \quad (E.20)$$
and

\[ \eta \Delta \lambda_1 = \frac{1}{R_1 R_2^2} \exp \left[ -2L \left( \alpha + \frac{1}{2L} \ln \left( \frac{1}{R_1 R_2^2 \epsilon \eta_0} \right) \right) \left( \frac{R'-1}{2} - \alpha \right) \right]. \]  \hspace{1cm} (E.21)

Setting the right sides Equations E.21 and E.7 equal then allows for solution for \( \Delta \lambda_1 \).

\[ \Delta \lambda_1 = \frac{\lambda \omega_0 (\beta^2 + 1)^{1/2}}{f \tan(\theta)} \left[ \left( \alpha + \frac{1}{2L} \ln \left( \frac{1}{R_1 R_2^2 \epsilon \eta_0} \right) \right) \left( \frac{R'-1}{2} - \alpha \right) \right]^{1/2} \]  \hspace{1cm} (E.22)

where \( \gamma \) is given by

\[ \gamma = \ln \left( \frac{\beta^2 + 1}{2 \beta R_1 R_2^2 \epsilon} \right) \]  \hspace{1cm} (E.23)

Several numerical values are needed for the evaluation of Equation E.22. \( \omega_0 \) is calculated with use of the fundamental eigenvalue equation for TM modes in a symmetric waveguide:

\[ \tan \left( \frac{\kappa d}{2} \right) = \frac{n_2^2 \Gamma}{n_1^2 \kappa} \]  \hspace{1cm} (E.24)

where \( \kappa \) is the complex waveguide propagation constant, \( d \) is the active region thickness, \( n_2 \) is the active region index of refraction, where \( \Gamma \) is given by

\[ \Gamma^2 = \chi^2 - n_1^2 k_o^2 \]  \hspace{1cm} (E.25)

and where \( n_1 \) is the waveguide cladding layer index of refraction, \( \chi \) is \( \frac{2\pi}{\lambda} \) in the waveguide, and \( k_o \) is given by.
\[ k_o = 2 \frac{\pi}{\lambda_o} \]  \hspace{1cm} (E.26)

where \( \lambda_o \) is the free-space lasing wavelength. Numerical solution of the transcendental equation E.24 gives \( \omega_o = 0.2 \mu m \). A diffraction-limited spotsize for the off-axis parabolic mirror used in the present project may be calculated to be \( \approx 0.9 \mu m \). Thus, \( \beta \) is \( \approx 4.5 \).

Numerical values for the various parameters of Equation E.22 are as follows:

\[ \lambda = 1.65 \mu m, \]

\[ \omega_o = 0.2 \mu m, \]

\[ \beta = 4.5, \]

\[ f = 35 \text{mm}, \]

\[ \tan(\theta) = 0.56, \]

\[ L = 400 \mu m, \]

\[ R_1 = 0.26, \]

\[ R_m = 0.95, \]

\[ \epsilon = 0.70, \]

\[ \eta_o = \frac{2\beta}{\left(\beta^2 + 1\right)} = 0.42, \]

\[ \gamma = 2.6, \]

\[ \alpha \approx 100 \text{ cm}^{-1}, \]

and

\[ R' = 2 \text{ to } 3. \]

Substitution into Equation E.22 gives a numerical value

\[ \Delta \lambda \frac{1}{2} = 1.0 \text{ to } 1.5 \text{ Angstroms.} \]
APPENDIX F

This appendix is a source listing of the Basic language source program CAVITY. The program is documented in several OGC CH₄ laboratory notebooks. The most recent version of the program is located in lab book CH₄-7. The uses of the program are explained in Chapter 6.
1 DEFINE FILE #4='X', ASC SEP
2 DEFINE FILE #5='Y', ASC SEP
3 DEFINE FILE #6='Z', ASC SEP
4 DIM W(100)
5 B$='YES'
6 K=3.1415926536/180
7 Q=0
8 DEFINE FILE #3='IMAGE', ASC SEP
9 DEFINE FILE #1='ROTPOS', ASC SEP
10 DEFINE FILE #2='SPOTSZ'
11 PRINT 'INPUT TILT OF LASER TO Z AXIS (90 DEGREES)'
12 INPUT H3
13 PRINT 'INPUT MAX ANGLE SEPARATION OF RAYS (DEGREES) PER AND'
14 PRINT 'PARALLEL TO ACTIVE REGION'
15 INPUT H4,H5
16 PRINT 'DO YOU WANT RAYS DRAWN'
17 INPUT A$
18 PRINT 'DO YOU WISH RANDOM RAYS FOR 100 RAYS'
19 INPUT D$
20 PRINT 'DO YOU WISH WIDEST RAYS DRAWN'
21 INPUT C$
22 IF D$='YES' THEN 70
23 DEFINE FILE #7='SPOTSTAT', ASC SEP
24 PRINT 'INPUT NUMBER OF PREVIOUS SPOTSTAT POINTS TO BE BYPASSED'
25 U$=20.61
26 U8=28.88
27 INPUT R
28 REM CONSTANTS FOR GAUSSIAN IMPROVEMENT ROUTINE-ABRAMOWITZ
29 REM AND STEGUN PAGE 953 CORRECTED
30 A(0)=-.98746
31 A(2)=.003943
32 A(4)=.474E-05
33 A(6)=-.102E-07
34 A(8)=1.213E-07
35 P$=3.14159
36 GOTO 105
37 PRINT 'DO YOU WISH AUTOMATIC ANGLE READING FOR START PT.'
38 INPUT F$
39 IF F$='YES' THEN 105
40 PRINT 'INPUT NUMBER OF ANGLES TO BE READ'
41 INPUT J
42 PRINT 'INPUT PARABOLA FOCAL LENGTH IN MM.'
43 INPUT F
44 REM GJ IS GAUSSIAN VARIABLE COUNTER
45 GJ=1
46 PRINT 'INPUT Z COORDINATE OF GRATING'
47 INPUT Z9
48 L=0
49 PRINT 'INPUT YO,ZO START PTS. WITH FOCUS AT (O,O,F)
50 INPUT Y0,Z0
51 PRINT 'INPUT X COORDINATE OF LASER FACET'
52 INPUT W7
53 X0=TAN(K$*(-H3))*Z0-F)+W7
54 IF D$='YES' THEN 191
55 IF B$='YES' THEN 205
56 REM
181. REM
182. REM FIND LINE 1
183. REM E0 IS END VALUE OF T
184. REM A8, B8, C8 ARE DIRECTION COSINES FOR LINE 1
185. IF F$<>'YES' THEN 201
186. GOTO 193
187. GOSUB 5000
188. GOTO 204
189. READ H1, H2
190. GOTO 204
201. PRINT 'INPUT INITIAL RAY DIVERGENCE FROM FACET NORMAL'
202. PRINT 'PERPENDICULAR, PARALLEL TO ACT. REGION DEGREES'
203. INPUT H1, H2
204. GOSUB 3500
205. A=AB
206. B=BB
207. C=CB
208. X=XO
209. Y=YO
210. Z=ZO
211. GOSUB 4000
212. E=E0
213. R=A8
214. S=B8
215. C=C8
216. IF A$<>'YES' THEN 240
217. FOR T=0.0..E0.E0/100
218. U=X+TO*A
219. V=Y+TO*B
220. W=Z+TO*C
221. GOSUB 6000
222. NEXT TO
223. U=X+E0*A
224. V=Y+E0*B
225. W=Z+E0*C
226. REM
227. REM FIND LINE 2
228. REM E1 IS END VALUE OF T
229. REM A1, B1, C1 ARE DIRECTION COSINES
230. X=U
231. Y=V
232. Z=W
233. S0=2*SQRT(F*Z+F-2)
234. H1=X/S0
235. H2=Y/S0
236. H3=-2*F/S0
237. A=A8
238. B=BB
239. C=CB
240. GOSUB 4500
241. A1=A8
242. B1=BB
243. C1=CB
244. E1=(29-Z)/C1
245. IF A$<>'YES' THEN 390
360 FOR T1=0,E1,E1/100
370 U=X+T1*A1
371 V=Y+T1*B1
372 W=Z+T1*C1
373 GOSUB 6000
380 NEXT T1
390 U=X+T1*A1
391 V=Y+T1*B1
392 W=Z+T1*C1
400 REM
409 REM
500 REM FIND LINE 3
501 REM E2 IS END VALUE OF T
502 REM A2,B2,C2 ARE DIRECTION COSINES
510 X=U
511 Y=V
512 Z=W
520 A=A1
521 B=B1
522 C=-C1
525 GOSUB 4000
530 X2=X
531 E2=E
540 IF A='YES' THEN 580
550 FOR T2=0,E2,E2/100
560 U=X+T2*A
561 V=Y+T2*B
562 W=Z+T2*C
563 GOSUB 6000
570 NEXT T2
580 U=X+E2*A
581 V=Y+E2*B
582 W=Z+E2*C
638 REM
699 REM
700 REM FIND LINE 4
701 REM E3 IS END VALUE FOR T
702 REM A3,B3,C3 ARE DIRECTION COSINES
710 X=U
711 Y=V
712 Z=W
720 S0=2*SQR(F+Z+F^-2)
740 H=X/S0
741 H2=Y/S0
742 H3=Z/F/S0
720 GOSUB 4500
750 A3=69
761 B3=69
772 C3=C9
765 E3=(TAN(K*(-H3))*(Z-F)-X)/(A3-TAN(K*(-H3))*C3)
767 IF A='YES' THEN 800
770 FOR T3=0,E3,E3/100
780 U=X+T3*A3
781 V=Y+T3*B3
782 W=Z+T3*C3
783 GOSUB 6000
ROUTINE TO CALCULATE THE STANDARD DEVIATION AND FULL WIDTH HALF MAXIMUM (FWHM) SIZE OF THE RETURNED SPOT IF RANDOM (GAUSSIAN DENSITY) INITIAL ANGLES ARE USED

CALCULATE STANDARD DEVIATION IN VARIATES X,Y

X1=SQR(N*S7-S6^2)/N
X2=SQR(N*S9-S8^2)/N

CONVERT S.D. TO FWHM DIAMETERS ASSUMING GAUSSIAN DIST

X1=X1*2*SQR(-2*LOG(0.5))
X2=X2*2*SQR(-2*LOG(0.5))

PRINT 'FWHM SPOT SIZE PERP. TO JUNCTION IN MICRONS'
PRINT X1
PRINT 'FWHM SPOT SIZE PARALLEL TO JUNCTION IN MICRONS'
PRINT X2

FOR I=1,2.R
IF R=0 THEN B210
READ #7,R9
NEXT I

WRITE #7,W7,X1
WRITE #7,W7,X2

DATA -35.0,-25.0,-15.0,0.0,15.0,25.0,35.0
DATA -35.0,-25.0,-15.0,0.0,15.0,25.0,35.0,-20
DATA -35.0,-25.0,-15.0,0.0,15.0,25.0,35.0,20
END
790 NEXT T4
800 U=E3*A3
801 V=E3*B3
802 W=Z+E3*C3
897 REM
898 REM FINAL PTS IN LASER FACET PLANE
899 REM
900 X4=W
901 Y4=W
902 Z4=W
993 IF B#='YES' THEN 1010
1000 PRINT X0,Y0,Z0
1001 PRINT X4,Y4,Z4
1002 PRINT
1010 WRITE @2,X0,Y0,Z0,A0,B0,C0
1011 WRITE @2,X4,Y4,Z4
1020 WRITE @3,1000*(Z4-F)/COS(K*H3),Y4*1000
1022 IF D#='YES' THEN 191
1030 IF F#='YES' THEN 6500
1050 PRINT ' DO YOU WISH NEW ANGLES'
1051 INPUT B#
1060 PRINT ' DO YOU WISH NEW STARTING PT'
1061 INPUT C#
1070 IF B#='YES' THEN IF C#='YES' THEN 115
1080 IF B#='YES' THEN IF C##='YES' THEN 201
1092 IF C#='YES' THEN 115
1100 IF A##='YES' THEN 9999
1507 GOSUB 6000
1520 REM
1521 REM
1522 REM CALCULATE LINES FOR WIDEST RAYS IN X,Z PLANE
1523 REM STARTING AT FOCUS,
1524 REM
1530 X0=0
1531 Y0=0
1532 Z0=F
1540 H1=H4
1541 IF Q<1.5 THEN 1700
1542 H2=H5
1550 GOSUB 3500
1555 X=X0
1556 Y=Y0
1557 Z=Z0
1558 A=H8
1559 B=H8
1560 C=C8
1570 GOSUB 4000
1585 FOR T4=0,E,E/100
1600 U=X+T4*A
1601 V=Y+T4*B
1602 W=Z+T4*C
1603 IF D#='YES' THEN 1610
1604 IF B#='YES' THEN 1610
1605 GOSUB 6000
1610 NEXT T4
1612 IF Q<.5 THEN 1620
X6 = U
Y6 = V
Z6 = W
GOTO 1630
X5 = U
Y5 = V
Z5 = W
H1 = -H4
Q = Q + 1
GOTO 1541
REM
REM CALC. PTS ON PARABOLA BETWEEN EXTREME RAYS IN
REM XZ PLANE
REM
T = \(1.1 \times X6 - .9 \times X6 / (9 \times X6 - 1.1 \times X5) / 100\)
W = T \(\times (4 \times F)\)
U = T
V = 0
GOSUB 6000
NEXT T
REM
REM CALCULATE PTS ON GRATIN
REM
FOR T = X5 . . . X6 . . . (X6 - X5) / 100
W = Z9
V = 0
U = T
GOSUB 6000
NEXT T
GOTO 7000
REM
REM MISC. ROUTINES
REM
CALCULATE INITIAL DIRECTION COSINES
H3 = H3 * K
H1 = H1 * K
H2 = H2 * K
AB = \(\cos(H1) \times \cos(H3) - \sin(H1) \times \sin(H3)\)
BB = \(\cos(H1) \times \sin(H2)\)
CB = \(\cos(H1) \times \sin(H2) \times \sin(H3) + \sin(H1) \times \cos(H3)\)
H1 = H1 / K
H2 = H2 / K
H3 = H3 / K
RETURN
REM
REM FIND END PT FOR T WHEN APPROACHING PARABOLA
REM 4000 IF A^2+B^2>F/10000 THEN 4010
REM 4003 E=(X^2+Y^2)/(4*F*C)-Z^2
REM 4004 GOTO 4060
REM 4010 S0=A^2+B^2
REM 4020 S1=2*F*C-B*Y-A*X
REM 4030 S2=S1^2
REM 4040 S3=S0*(X^2+Y^2-4*F*X)
REM 4050 E=(S1+SQR(S2-S3))/S0
REM 4060 RETURN
REM 4498 REM
REM 4499 REM
REM 4500 REM CALCULATE DIRECTION COSINES AFTER PARABOLA
REM 4501 REM
REM 4510 A9=(1-2*H1^2)*A-2*N1*N2*B-2*M1*N3*C
REM 4520 B9=-2*M1*N2*A+(1-2*H2^2)*B-2*N2*N3*C
REM 4530 C9=-2*M1*N3*A-2*N2*N3*B+(1-2*H3^2)*C
REM 4540 RETURN
REM 4598 REM
REM 5000 REM ROUTINE TO GENERATE 100 GAUSSIAN RANDOM INITIAL ANGLES
REM 5001 REM
REM 5100 IF G1>100 THEN 1520
REM 5200 U1=RND(J)
REM 5300 U2=RND(J)
REM 5320 U3=-(2*LOG(U1))^2.*COS(2*PI*U2)
REM 5330 U4=-(2*LOG(U1))^2.*SIN(2*PI*U2)
REM 5340 H1=0
REM 5350 H2=0
REM 5399 REM LOOP FOR IMPROVEMENT ROUTINE
REM 5400 FOR K9=0.8,2
REM 5410 H1=H1+A(K9)*U3*K9
REM 5420 H2=H2+A(K9)*U4*K9
REM 5430 NEXT K9
REM 5440 H1=H1+U3*U8
REM 5450 H2=H2+U4*U9
REM 5454 REM CHECK IF INITIAL GAUSSIAN ANGLE FALLS ON MIRROR
REM 5455 IF ABS(H1)>ABS(H4) THEN 5300
REM 5456 IF ABS(H2)>ABS(H5) THEN 5300
REM 5800 G1=G1+1
REM 5900 RETURN
REM 5998 REM
REM 6000 REM ROUTINE FOR LINE DRAWING ITERATION
REM 6001 REM
REM 6003 WRITE 04,U
REM 6004 WRITE 05,V
REM 6005 WRITE 06,W
REM 6006 L=L+1
REM 6007 RETURN
REM 6500 REM
REM 6501 REM
REM 6502 REM ROUTINE TO READ ANGLES AUTOMATICALLY
REM 6503 REM
REM 6510 J=J-1
REM 6515 IF J=0 THEN 1100
VITA

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Mr. DeFreez was an American Physical Society Graduate Industrial Intern to the Homer Research Laboratories of the Bethlehem Steel Corporation in 1979 and 1980. He holds a patent for a remote methane sensor as a result of work conducted there. He was an Assistant Professor of Physics and Mathematics at Sonoma State University during the spring semester of 1980. He recently spent three months as a Visiting Scientist at Xerox Palo Alto Research Center where he successfully demonstrated the first cleaved-coupled-cavity phased array laser.

In September 1980, he began his studies at Oregon Graduate Center. Since that time he has coauthored several technical publications and presented papers at several conferences.
PUBLICATIONS AND CONFERENCES


R. K. DeFreez, R. A. Elliott, J. S. Blakemore, B. I. Miller, J. H. McFee and R. J. Martin, High-Output Room Temperature Pulsed Operation for Broad Contact InP/In_{0.65}Ga_{0.35}As /InP Lasers Grown by Molecular Beam Epitaxy, J. Appl. Phys., 54, May 1983, 2177-2182